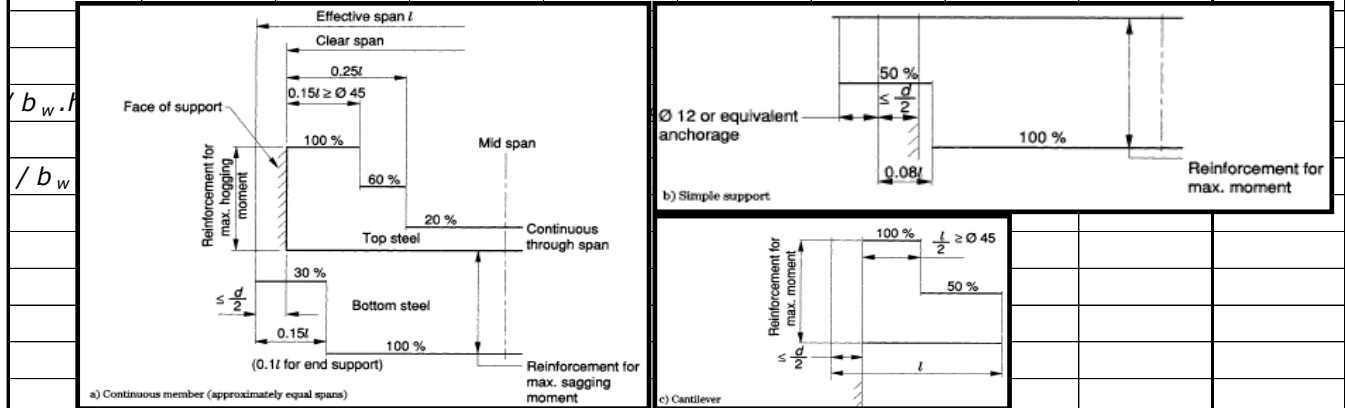
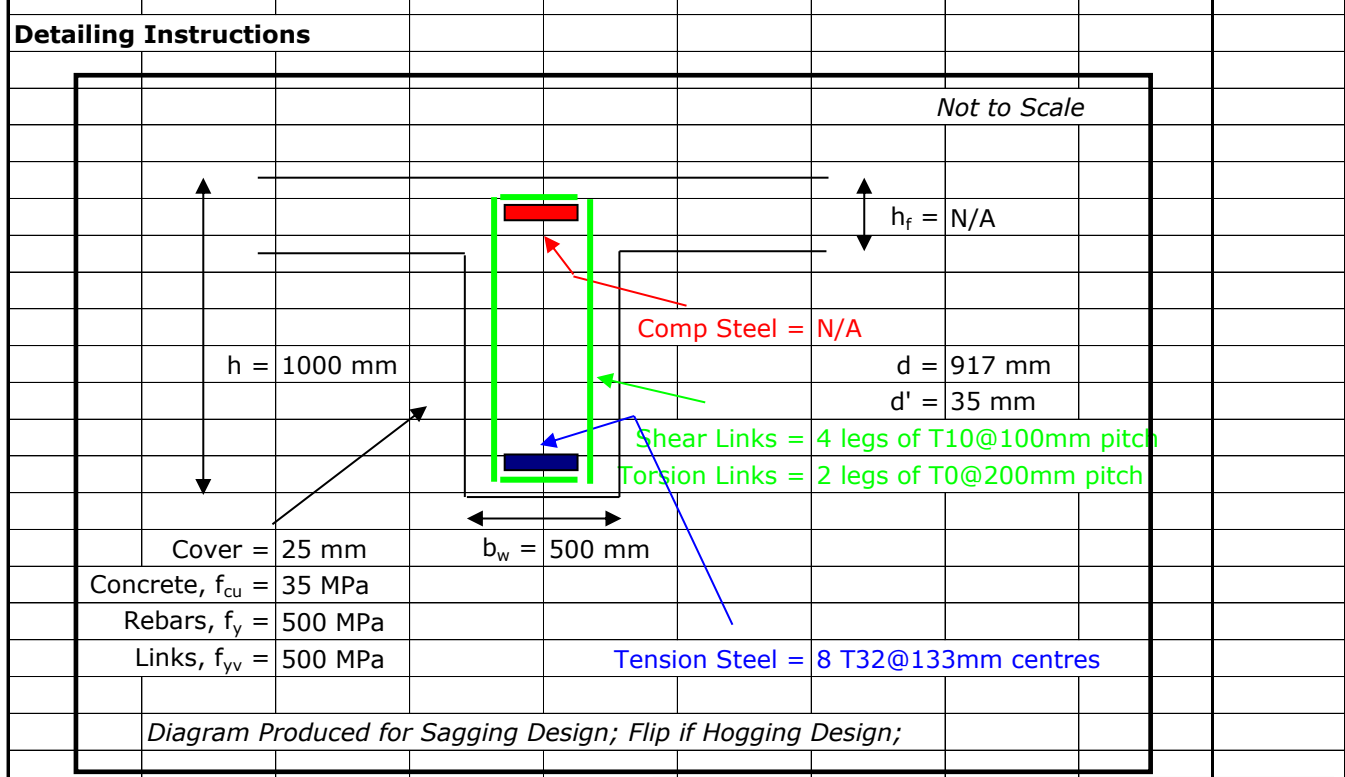
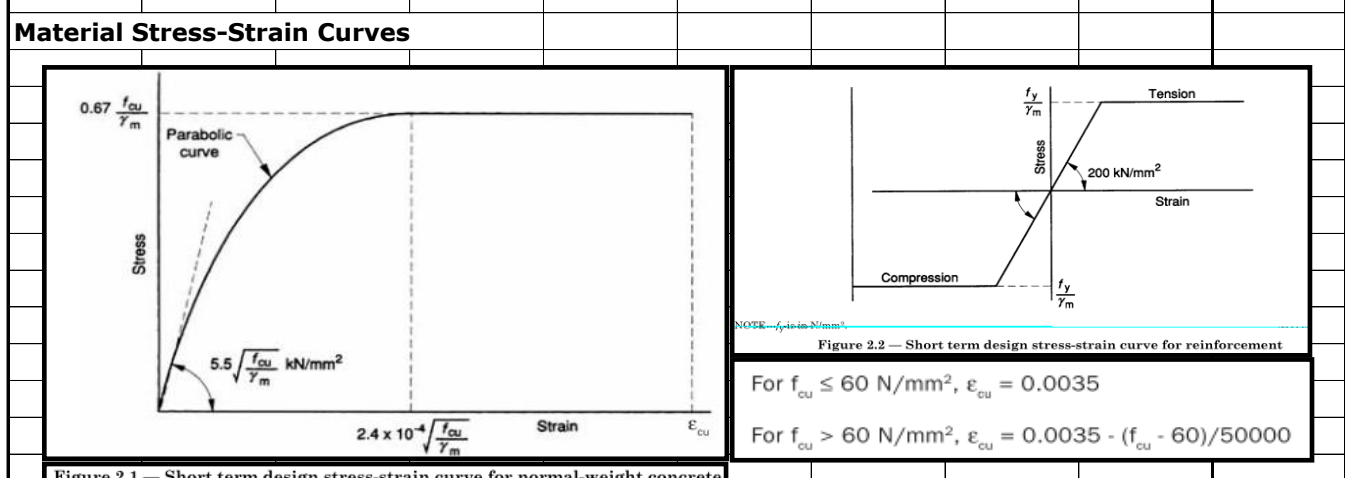


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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
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<b>Effects From Structural Analysis</b>				Do not adopt code equivalence		▼			
Design axial force, F (tension -ve and comp. +ve) (ensure $< 0.1f_{cu}b_w h$ )					0	kN	OK		
Design shear force, $V_d$					1170	kN			
Design bending moment, M					1849	kNm			
Design torsion moment, T					0	kNm			
<b>Material Properties</b>									
Characteristic strength of concrete, $f_{cu} / f_{ck}   f_c' (f_{cu} \leq 75 \text{ or } 105N)$					35	▼	28	▼	N/mm <sup>2</sup>
Yield strength of longitudinal steel, $f_y$					Higher	▼	500	▼	N/mm <sup>2</sup>
Yield strength of shear and torsion link steel, $f_{yv}$					Higher	▼	500	▼	N/mm <sup>2</sup>
<b>Section Dimensions</b>									
Span (effective width, deflection, long'l shear and deep beam calcs)					10.000	m			
Available beam spacing					1.000	m			
<i>(effective width calcs; usual spacing for interior beams; half for edge beams)</i>									
Beam section type and support condition					Rect - continuous		▼		
<i>(section type for bending, defl'n calcs; support condition for LTB restraint, eff width, defl'n, long'l shear calcs)</i>									
Ratio $\beta_b$ (1.0 for no moment redistribution, $\geq 0.70, \leq 1.30$ )					1.00		OK		
<b>Section Type and Support Condition Option Selection</b>									
<b>Downstand Beam</b>					<b>Upstand Beam</b>				
Support	Effect	Slab	Type	Defl'n	Support	Effect	Slab	Type	Defl'n
S/S	Sag	Precast	Rect-s/s	Yes	S/S	Sag	Precast	Rect-s/s	Yes
S/S	Sag	Insitu	T/L-s/s	Yes	S/S	Sag	Insitu	Rect-s/s	Yes
Cont.	Sag	Precast	Rect-cont.	Yes	Cont.	Sag	Precast	Rect-cont.	Yes
Cont.	Sag	Insitu	T/L-cont.	Yes	Cont.	Sag	Insitu	Rect-cont.	Yes
Cont.	Hog	Precast	Rect-cont.	N/A	Cont.	Hog	Precast	Rect-cont.	N/A
Cont.	Hog	Insitu	Rect-cont.	N/A	Cont.	Hog	Insitu	T/L-cont.	N/A
Cant.	Hog	Precast	Rect-cant.	Yes	Cant.	Hog	Precast	Rect-cant.	Yes
Cant.	Hog	Insitu	Rect-cant.	Yes	Cant.	Hog	Insitu	T/L-cant.	Yes
Overall depth, h (includes insitu slab thks; excludes precast slab thks; span/					1000	mm	OK		
Depth of flange, $h_f$ (bending flanged beam, longitudinal shear calcs)					200	mm			
Width (rectangular) or web width (flanged), $b_w$					500	mm			
Cover to all reinforcement, cover (usually 35 (C35) or 30 (C40) internal; 40					25	mm			
Add cover to tension steel (due to transverse steel layer(s)), $cover_{add,t}$					0	mm			
Add cover to compression steel (due to transverse steel layer(s)), $cover_{add,c}$					0	mm			
Effective depth to tension steel, $d = h - cover - \text{MAX}(\phi_{link,r}, \phi_{link,tr}, cover_{add,t}) - [$					917	mm			
Effective depth to compression steel, $d' = cover + \text{MAX}(\phi_{link,r}, \phi_{link,tr}, cover_{add,c})$					35	mm			
<b>Longitudinal Reinforcement Details</b>									
Tension steel reinforcement diameter, $\phi_t$					32	▼	mm		
Tension steel reinforcement number, $n_t$					8				
Tension steel area provided, $A_{s,prov} = n_t \cdot \pi \cdot \phi_t^2 / 4$					6434	mm <sup>2</sup>			
Compression steel reinforcement diameter, $\phi_c$ (where applicable)					None	▼	mm		
Compression steel reinforcement number, $n_c$					0				
Compression steel area provided, $A_{s,prov}' = n_c \cdot \pi \cdot \phi_c^2 / 4$					0	mm <sup>2</sup>			
Number of layers of tension steel, $n_{layers,tens}$					2	layer(s)			
Spacer for tension steel, $s_{r,tens} (\geq \text{MAX}(\phi_{tr}, 25\text{mm}))$					32	mm	OK		
Number of layers of compression steel, $n_{layers,comp}$					1	layer(s)			
Spacer for compression steel, $s_{r,comp} = \text{MAX}(\phi_{cr}, 25\text{mm})$					25	mm			

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Member Design - RC Beam					Made by	XX	Date
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							BS8110
<b>Shear Reinforcement Details</b>							
Shear link diameter, $\phi_{link}$					10	mm	
Number of shear links in a cross section, i.e. number of legs, $n_{leg}$					4		
Area provided by all shear links in a cross-section, $A_{sv,prov} = \pi \cdot \phi_{link}^2 / 4 \cdot n_{leg}$					314	mm <sup>2</sup>	
Pitch of shear links, S					100	mm	
<b>Torsion Reinforcement Details</b>							
Torsion link diameter, $\phi_{link,t}$					None	mm	
Number of torsion links in a cross section, i.e. number of legs, $n_{leg,t} = 2$					2		
Area provided by all torsion links in a cross-section, $A_{sv,prov,t} = \pi \cdot \phi_{link,t}^2 / 4 \cdot n_{leg,t}$					0	mm <sup>2</sup>	
Pitch of torsion links, $S_t$					200	mm	
Note that further longitudinal steel $A_{s,t}$ must					0	0	0
					0	mm <sup>2</sup>	
<b>Utilisation Summary</b>							
<b>Item</b>				<b>UT</b>		<b>Remark</b>	
RB tens steel				86%	79%	86%	OK
RB comp steel				N/A	N/A	N/A	N/A
RB % min tens reinf.				10%	20%	20%	OK
RB % min comp reinf.						N/A	N/A
RB % max tens and comp reinf.						32%	OK
FB tens steel						N/A	N/A
FB comp steel						N/A	N/A
FB % min tens reinf.						N/A	N/A
FB % min comp reinf.						N/A	N/A
FB % max tens and comp reinf.						N/A	N/A
RB shear ultimate str				54%	57%	77%	OK
RB shear design capa				72%	42%	96%	OK
RB torsion ultimate str				0%	0%	0%	OK
RB torsion design cap				0%	0%	0%	OK
RB shear and torsion				54%	57%	77%	OK
RB or FB deflection requirements						49%	OK
<b>Total utilisation rectangular beam</b>				<b>96%</b>		<b>OK</b>	
<b>Total utilisation rectangular beam (excluding def</b>				<b>96%</b>		<b>OK</b>	
<b>Total utilisation flanged beam</b>				<b>N/A</b>		<b>N/A</b>	
<b>Detailing requirements</b>				<b>OK</b>			
<i>Note RB = rectangular beam, FB = flanged beam;</i>							
% Tension reinforcement (rectangular)						1.29	%
% Compression reinforcement (rectangular)						N/A	%
% Tension reinforcement (flanged)						N/A	%
% Compression reinforcement (flanged)						N/A	%
Estimated steel reinforcement quantity (125 – 160kg/m <sup>3</sup> )						158	kg/m <sup>3</sup>
$7850 \cdot [(A_{s,prov} + A_{s,prov'}) / (b_w \text{ or } b) \cdot (h \text{ or } h_f) + (A_{sv,prov} \cdot (h+anc.) / S + A_{sv,prov,t} \cdot (h+b_w+anc.) / S_t)]$							
Estimated steel reinforcement quantity (125 – 160kg/m <sup>3</sup> )						222	kg/m <sup>3</sup>
$11000 \cdot [(A_{s,prov} + A_{s,prov'}) / (b_w \text{ or } b) \cdot (h \text{ or } h_f) + (A_{sv,prov} \cdot (h+anc.) / S + A_{sv,prov,t} \cdot (h+b_w+anc.) / S_t)]$							
[Note that steel quantity in kg/m <sup>3</sup> can be obtained from 110.0 x % rebar];							
Material cost: concrete, c				315	units/m <sup>3</sup>	steel, s	4600
Reinforced concrete material cost = [c+(est. rebar quant).s].(b <sub>w</sub>				667		units/m	
Ductility of failure mechanism				Consider	<b>Section Under Reinforced</b>		
Rectangular beam crack width				101%			<b>NOT OK</b>
Max LTB stability (compression flange) restraints spacing, L <sub>LTB</sub>				30.0		m	
<i>Note s/s / cont L<sub>LTB</sub> = MIN (60(b<sub>w</sub> or b), 250(b<sub>w</sub> or b)<sup>2</sup>/d) and cant L<sub>LTB</sub> = MIN (25b<sub>w</sub>, 100b<sub>w</sub><sup>2</sup></i>							

				<i>BS8110</i>
<b>Material Stresses</b>				
Axial stress, $F/b_w h$				<b>0.00</b> N/mm <sup>2</sup>
Shear stress, $V_d/b_w d$				<b>2.55</b> N/mm <sup>2</sup>
Bending stress, $6M/(b_w \text{ or } b) \cdot d^2$				<b>26.39</b> N/mm <sup>2</sup>
Torsion stress, $2T/((h_{min})^2(h_{max}-h_{min}/3))$				<b>0.00</b> N/mm <sup>2</sup>



(d);

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<b>Additional Longitudinal Shear Rectangular or Flanged Beam Utilisation Summary</b>									
Longitudinal shear between web and flange					Consider only if applicable		▼		
Longitudinal shear within web					Consider only if applicable		▼		
Length under consideration, Δx (span/2 s/s, span/4 cont, span cant)						2500	mm		
Applicability of longitudinal shear design					<b>Applicable</b>				
<b>Longitudinal Shear Between Web and Flange (EC2)</b>									
Longitudinal shear stress limit to prevent crushing					32%			OK	
Longitudinal shear stress limit for no transverse reinforcement					312%			NOT OK	
Required design transverse reinforcement per unit length					94%			OK	
<b>Longitudinal Shear Between Web and Flange (BS5400-4)</b>									
Longitudinal shear force limit per unit length					64%			OK	
Required nominal transverse reinforcement per unit length					38%			OK	
<b>Longitudinal Shear Between Web and Flange Mandatory Cr</b>					94%			OK	
<b>Longitudinal Shear Within Web (EC2)</b>									
Longitudinal shear stress limit					49%			OK	
<b>Longitudinal Shear Within Web (BS8110)</b>									
Longitudinal shear stress limit for no nominal / design vertical rei					110%			NOT OK	
Required nominal vertical reinforcement per unit length					24%			OK	
Required design vertical reinforcement per unit length					94%			OK	
<b>Longitudinal Shear Within Web (BS5400-4)</b>									
Longitudinal shear force limit per unit length					79%			OK	
Required nominal vertical reinforcement per unit length					24%			OK	
<b>Longitudinal Shear Within Web Mandatory Criteria</b>					94%			OK	
<b>Additional Deep Beam Rectangular Beam Utilisation Summary</b>									
Deep beam design					Consider only if applicable		▼		
Span to depth ratio, span / h					10.00			OK	
Applicability of deep beam design					<b>Not Applicable</b>				
Concrete type					Normal weight		▼		
Horizontal shear link diameter, φ <sub>link,h</sub>					None		▼		mm
Number of horizontal shear links in a horizontal section, i.e. number of legs,					0				
Pitch of horizontal shear links, S <sub>h</sub>					0			mm	
Clear distance from edge of load to face of support, a <sub>1</sub> o DL @ mid 0.625h					▼		N/A	mm	
Detailing requirements					<b>N/A</b>				
<b>Reynolds</b>									
Tension steel (deep beam)					N/A			N/A	
Tension steel zone depth, T <sub>zone</sub> (sag s/s, sag cont, hog cant)					N/A	mm			
Tension steel zone depth, T <sub>zone</sub> (hog cont)					N/A	mm			
Minimum breadth for deep beam, b <sub>w</sub>					N/A	mm		N/A	
Shear ultimate force (deep beam)					N/A			N/A	
Shear design capacity (deep beam)					N/A			N/A	
<b>CIRIA Guide 2</b>									
Bending ultimate moment (deep beam)					N/A			N/A	
Tension steel (deep beam)					N/A			N/A	
Tension steel zone depth, T <sub>zone</sub> (sag s/s, sag cont, hog cant)					N/A	mm			
Tension steel zone depth, T <sub>zone</sub> (hog cont) upper band					N/A	N/A	mm		
Tension steel zone depth, T <sub>zone</sub> (hog cont) lower band					N/A	N/A	mm		
Shear ultimate force (deep beam)					N/A			N/A	
Shear design capacity (deep beam)					N/A			N/A	

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<b>Bending Rectangular Beam (Singly or Doubly Reinforced) (BS8110)</b>						
<p>Figure 3.3 (amended) – Simplified stress block for concrete at ultimate limit state</p>						
$M_u = K' f_{cu} b d^2$		Note b here is $b_w$ ;		2296	kNm	
Ratio, $K'$				0.156		
$\frac{0.90}{\beta_b} \leq 1.10$	$K' =$	0.156 for $f_{cu} \leq 60 \text{ N/mm}^2$		0.156	mm	3.4.4.4 BC
		0.120 for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
		0.094 for $75 < f_{cu} \leq 105 \text{ N/mm}^2$ [ $\beta_b = 1.0$ ]		N/A	mm	3.4.4.4 BC
$\frac{0.90}{\beta_b} > 1.10$	$K' =$	0.402( $\beta_b - 0.4$ ) - 0.18( $\beta_b - 0.4$ ) <sup>2</sup> , for $f_{cu} \leq 60 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
		0.357( $\beta_b - 0.5$ ) - 0.143( $\beta_b - 0.5$ ) <sup>2</sup> for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
Note the expression for $K'$ ensures that the section remains ductile i.e. ensuring that failure occurs with the gradual yielding of the tension steel and not by a sudden catastrophic compression failure of the concrete;						
If: $M < M_u \rightarrow$ no compression steel				VALID		
$K = M/bd^2 f_{cu}$		Note b here is $b_w$ ;		0.126		
To scheme beam, choose $d$ such that $K = M/(b_w d^2 f_{cu}) < K'$ (0.156 for $\beta_b = 1.0$ and NSC) for no compression steel, i.e. $d > 823$ and $h > 906$ mm						
$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right\}$		$z \leq 0.95d$		763	mm	
Depth of neutral axis, $x \leq x_{limit}$		342		459	mm	OK
Neutral axis, $x$	$x =$	$(d - z)/0.45$ , for $f_{cu} \leq 60 \text{ N/mm}^2$		342	mm	3.4.4.4 BC
		$(d - z)/0.40$ , for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
		$(d - z)/0.36$ , for $75 < f_{cu} \leq 105 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
Neutral axis limit, $x_{limit}$	$0.90 \leq \frac{\beta_b}{1.10}$	$x \leq 0.5d$ for $f_{cu} \leq 60 \text{ N/mm}^2$		459	mm	3.4.4.4 BC
		$x \leq 0.4d$ for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
		$x \leq 0.33d$ , for $75 < f_{cu} \leq 105 \text{ N/mm}^2$ [ $\beta_b = 1.0$ ]		N/A	mm	3.4.4.4 BC
		$x \leq (\beta_b - 0.4)d$ for $f_{cu} \leq 60 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
$0.90 > \frac{\beta_b}{1.10}$		$x \leq (\beta_b - 0.5)d$ for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
Tension steel	$A_s = \frac{M}{(0.95 f_y) z}$ , $f_y \leq 460 \text{ N/mm}^2$		5544	mm <sup>2</sup>	Foreword	
Back-analysis of $x$ in $(0.67 f_{cu}/1.5) \cdot (s \cdot b_w) = (f_y/1.05) \cdot (A_{s,prov})$ , $f_y \leq 460$		401		mm	OK	
$s =$	0.9x for $f_{cu} \leq 60 \text{ N/mm}^2$ ;		0.90x	mm	3.4.4.4 BC	
	0.8x for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC	
	0.72x for $75 < f_{cu} \leq 105 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC	
Note for an under reinforced section, require $x \leq x_{limit}$ for yielding of tension steel;						

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If: $M > M_u \rightarrow$ compression steel required					N/A		
To scheme beam, with compression steel, choose $d$ such that $K = M/(b_w d^2 f_{cu}) < 10/f_{cu}$							
for non-excessive comp steel, i.e. $d >$					608	and $h >$	691 mm
$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K'}{0.9}} \right\}$					N/A mm		
Depth of neutral axis, $x \leq x_{limit}$					N/A	$\leq$	N/A mm
Neutral axis	axis, $x$	$x =$	$(d - z)/0.45$ , for $f_{cu} \leq 60$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
			$(d - z)/0.40$ , for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
			$(d - z)/0.36$ , for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
Neutral axis	limit, $x_{limit}$	$0.90 \leq \beta_b \leq 1.10$	$x \leq 0.5d$ for $f_{cu} \leq 60$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
			$x \leq 0.4d$ for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
			$x \leq 0.33d$ , for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup> $\beta_b = 1.0$		N/A	mm	3.4.4.4 BC
2	2	$0.90 < \beta_b < 1.10$	$x \leq (\beta_b - 0.4)d$ for $f_{cu} \leq 60$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
			$x \leq (\beta_b - 0.5)d$ for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC
2	2	2	Compression steel $A_{s'} = \frac{M - K' f_{cu} b d^2}{0.95 f_y (d - d')}$ , $f_y \leq 460$ N/mm <sup>2</sup>		N/A	mm <sup>2</sup>	Foreword
2	2	2	Tension steel $A_s = \frac{M_u}{0.95 f_y z} + A_{s'}$ , $f_y \leq 460$ N/mm <sup>2</sup>		N/A	mm <sup>2</sup>	Foreword
If $d' > \left(1 - \frac{f_y}{735}\right) x$ , use $700 \left(1 - \frac{d'}{x}\right)$ in lieu of $0.95 f_y$ , $f_y \leq 460$ N/mm <sup>2</sup>					N/A		Foreword
Back-analysis of $x$ in $(0.67 f_{cu}/1.5) \cdot (s \cdot b_w) + (f_y/1.05) \cdot (A_{s,prov'}) = (f_y/1$					N/A	mm	N/A
s =		0.9x for $f_{cu} \leq 60$ N/mm <sup>2</sup> ; 0.8x for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup> 0.72x for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup>		N/A	mm	3.4.4.4 BC	
Note for an under reinforced section, require $\epsilon_{st} = \epsilon_{cc}(d-x)/x \geq \epsilon_y$ for yielding of tension steel and $\epsilon_{sc} = \epsilon_{cc}(x-d')/x \geq \epsilon_y$ for yielding of compression steel, where $\epsilon_{cc} = 0.0035$ for $f_{cu} \leq 60$ N/mm <sup>2</sup> and $\epsilon_{cc} = 0.0035 - (f_{cu} - 60)/50000$ for $f_{cu} > 60$ N/mm <sup>2</sup> and $\epsilon_y = (f_y/1.05)/E_s$ ;							
Tension steel area provided					6434	mm <sup>2</sup>	
Tension steel area provided utilisation					86%		OK
Compression steel area provided					N/A	mm <sup>2</sup>	
Compression steel area provided utilisation					N/A		N/A
% Min tension reinforcement					1.29	%	TR49
% Min tension reinforcement ( $\geq 0.0024 b_w h$ G250; $\geq \text{MAX}(0.0013, 0.0013(f_{cu}/40)^{2/3}) \cdot b_w h$ G							
% Min tension reinforcement utilisation					10%		OK
% Min compression reinforcement ( $\geq 0.002 b_w h$ )					N/A	%	
% Min compression reinforcement utilisation					N/A		N/A
% Max tension reinforcement ( $\leq 0.04 b_w h$ )					1.29	%	
% Max tension reinforcement utilisation					32%		OK
% Max compression reinforcement ( $\leq 0.04 b_w h$ )					N/A	%	
% Max compression reinforcement utilisation					N/A		N/A
% Max tension or compression reinforcement utilisation					32%		OK
2							
2							
2							

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Member Design - RC Beam				Made by	XX	Date
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<b>Bending Rectangular Beam (Singly or Doubly Reinforced) (ACI318)</b>						
<b>Singly Reinforced Rectangular Section</b>		<b>Doubly Reinforced Rectangular Section</b>				
Required nominal flexural strength coefficient of resistance, $R_n = M^* / \phi b_w d^2$				4.89	N/mm <sup>2</sup>	
Strength reduction factor for tension-controlled sections, $\phi = 0.90$				0.90		
Ratio of $A_s$ to $b_w d$ , $\rho_w = 0.85f'_c/f_y \cdot [1 - \sqrt{1 - 2R_n/(0.85f'_c)}]$ , $f_y \leq 550\text{N/mm}^2$				1.11	%	
Tension steel, $A_s = \text{MAX}(\rho_w b_w d, A_{s,\text{min}})$				5070	mm <sup>2</sup>	
$A_{s,\text{min}} = \text{MAX}(0.25b_w d \sqrt{f'_c}/f_y, 1.4b_w d/f_y)$ , $f_y \leq 550\text{N/mm}^2$				1284	mm <sup>2</sup>	
Factor, $\beta_1 = \text{MAX}(\text{MIN}(0.85 - (0.05/7) \cdot (f'_c - 28), 0.85), 0.65)$				0.85		
<i>Note <math>\beta_1</math> is the factor relating depth of equivalent rectangular compressive stress block to neutral axis depth;</i>						
Depth of equivalent rectangular stress block, $a = A_s \cdot f_y / (0.85f'_c \cdot b_w)$ , $f_y \leq 550\text{N/mm}^2$				213	mm	
Distance, $c = a/\beta_1$				251	mm	
<i>Note c is the distance from extreme compression fiber to neutral axis (for singly reinforced section);</i>						
Distance, $d_t = h - \text{cover} - \text{MAX}(\phi_{\text{link}}, \phi_{\text{link},tr}, \text{cover}_{\text{add},t}) - \phi_t/2$				949	mm	
<i>Note <math>d_t</math> is the distance from extreme compression fiber to centroid of extreme layer of longitudinal tension steel</i>						
$\epsilon_t = 0.003(d_t/c - 1)$				0.008		
<i>Note <math>\epsilon_t</math> is the net tensile strain in extreme layer of longitudinal tension steel at nominal strength;</i>						
$\epsilon_t > 0.005$		→ no compression steel		VALID		
Tension steel, $A_s$				5070	mm <sup>2</sup>	
$0.004 < \epsilon_t \leq 0.005$		→ compression steel required		N/A		
Ratio of $A_s$ to $b_w d$ , $\rho_w = 0.319\beta_1 f'_c/f_y \cdot d_t/d$ , $f_y \leq 550\text{N/mm}^2$				N/A	%	
$R_{nt} = \rho_w f_y (1 - 0.59\rho_w f_y/f'_c)$ , $f_y \leq 550\text{N/mm}^2$				N/A	N/mm <sup>2</sup>	
<i>Note <math>R_{nt}</math> is the required nominal flexural strength coefficient of resistance for rectangular beam corresponding to <math>\epsilon_t = 0.005</math>;</i>						
$M_{nt} = R_{nt} b_w d^2$				N/A	kNm	
<i>Note <math>M_{nt}</math> is the required nominal flexural strength corresponding to <math>\epsilon_t = 0.005</math>;</i>						
$M_n' = M^*/\phi - M_{nt}$				N/A	kNm	
<i>Note <math>M_n'</math> is the required nominal flexural strength that need to be resisted by the compression reinforcement;</i>						
Distance, $c_t = 0.375d_t$				N/A	mm	
<i>Note <math>c_t</math> is the distance from extreme compression fiber to neutral axis (for doubly reinforced section);</i>						
Stress in compression reinforcement, $f'_s = 0.003E_s(1 - d_t/c_t) \leq f_y$ , $f_y \leq 550\text{N/mm}^2$				N/A	N/mm <sup>2</sup>	
Modulus of elasticity of reinforcement, $E_s = 200,000$				N/A	N/mm <sup>2</sup>	
Compression steel, $A'_s = M_n' / [f'_s(d - d_t)]$				N/A	mm <sup>2</sup>	
Tension steel, $A_s = \rho_w b_w d + M_n' / [f_y(d - d_t)]$ , $f_y \leq 550\text{N/mm}^2$				N/A	mm <sup>2</sup>	
$\epsilon_t \leq 0.004$		→ no valid solution		N/A		





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<b>Bending Flanged Beam (Singly or Doubly Reinforced)</b>							
		Simply supported	Continuous	Cantilever	For cantilevers, width shown is applicable for downstand beams as rect- sections. For upstand beams, T- or L- sections will apply with insitu		
T-Beam		$b_w + L / 5$	$b_w + L / 7.14$	$b_w$			
L-Beam		$b_w + L / 10$	$b_w + L / 14.29$	$b_w$			
		and $\leq$ (i) actual flange width, (ii) beam spacing					
Span					N/A	mm	
Depth of flange, $h_f$					N/A	mm	N/A
Effective width, $b = \text{MIN}(b_w + \text{function (span, section, structure), beam spacing (bending flanged beam, deflection calcs flanged beam)})$					N/A	mm	
$K = M/bd^2f_{cu}$					N/A		
$z = d \cdot [0.5 + (0.25-K/0.9)^{0.5}] \leq 0.95d$					N/A	mm	
Depth of compression stress block, $s = 2 \cdot (d-z)$ (applicable for all $f_{cu}$ )					N/A	mm	
<b>Compression Stress Block in Flange (<math>s \leq h_f</math>)</b>					N/A		
$M_u = K'f_{cu}bd^2$					N/A	kNm	
Ratio, $K'$					N/A		
	$\leq$	$\beta_b$	$\leq$	$0.156$ for $f_{cu} \leq 60 \text{ N/mm}^2$	N/A	mm	3.4.4.4 BC
	$0.90$	$\beta_b$	$\leq$	$0.120$ for $60 < f_{cu} \leq 75 \text{ N/mm}^2$	N/A	mm	3.4.4.4 BC
	$0.90$	$\beta_b$	$\leq$	$0.094$ for $75 < f_{cu} \leq 105 \text{ N/mm}^2$ [ $\beta_b = 1.0$ ]	N/A	mm	3.4.4.4 BC
	$\wedge$	$\beta_b$	$\wedge$	$0.402(\beta_b - 0.4) - 0.18(\beta_b - 0.4)^2$ , for $f_{cu} \leq 60 \text{ N/mm}^2$	N/A	mm	3.4.4.4 BC
	$0.90$	$\beta_b$	$\wedge$	$0.357(\beta_b - 0.5) - 0.143(\beta_b - 0.5)^2$ for $60 < f_{cu} \leq 75 \text{ N/mm}^2$	N/A	mm	3.4.4.4 BC
Note the expression for $K'$ ensures that the section remains ductile i.e. ensuring that failure occurs with the gradual yielding of the tension steel and not by a sudden catastrophic compression failure of the concrete;							
If: $M < M_u \rightarrow$ no compression steel					N/A		
$K = M/bd^2f_{cu}$					N/A		
To scheme beam, choose $d$ such that $K = M/(bd^2 f_{cu}) < K'$ ( $0.156$ for $\beta_b = 1.0$ and NSC)							
for no compression steel, i.e. $d >$					N/A	and $h >$	N/A mm
$z = d \left\{ 0.5 + \sqrt{0.25 - \frac{K}{0.9}} \right\}$					N/A	mm	
Depth of neutral axis, $x \leq x_{limit}$					N/A	$\leq$	N/A mm
Neutral axis	axis, $x$	$x =$	$(d - z)/0.45$ , for $f_{cu} \leq 60 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
			$(d - z)/0.40$ , for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
			$(d - z)/0.36$ , for $75 < f_{cu} \leq 105 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
Neutral axis	limit, $x_{limit}$	$\leq$	$x \leq 0.5d$ for $f_{cu} \leq 60 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
			$x \leq 0.4d$ for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
			$x \leq 0.33d$ , for $75 < f_{cu} \leq 105 \text{ N/mm}^2$ [ $\beta_b = 1.0$ ]		N/A	mm	3.4.4.4 BC
Neutral axis	limit, $x_{limit}$	$\wedge$	$x \leq (\beta_b - 0.4)d$ for $f_{cu} \leq 60 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
			$x \leq (\beta_b - 0.5)d$ for $60 < f_{cu} \leq 75 \text{ N/mm}^2$		N/A	mm	3.4.4.4 BC
Tension steel $A_s = \frac{M}{(0.95f_y)z}$ , $f_y \leq 460 \text{ N/mm}^2$					N/A	mm <sup>2</sup>	Foreword
Back-analysis of $x$ in $(0.67f_{cu}/1.5) \cdot (s \cdot b) = (f_y/1.05) \cdot (A_{s,prov})$ , $f_y \leq 460$					N/A	mm	N/A
$s =$					N/A	mm	3.4.4.4 BC
					N/A	mm	3.4.4.4 BC
					N/A	mm	3.4.4.4 BC
Note for an under reinforced section, require $x \leq x_{limit}$ for yielding of tension steel;							



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<b>Compression Stress Block in Web (<math>s &gt; h_f</math> AND <math>h_f \leq \{0.45, 0.36, 0.30\}</math>)</b>						<b>N/A</b>
Note simplified method as equations within this section only valid for $\beta_b \geq 0.90$ and $\leq 1.10$ as $x = 0.5d$ ;						
$h_f < 0.45d$ for $f_{cu} \leq 60$ N/mm <sup>2</sup> ; or $h_f < 0.36d$ for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup> ; or $h_f < 0.30d$ for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup> and no moment redistribution.						cl.3.4.4.4 BC cl.3.4.4.4 BC cl.3.4.4.4 BC
2	$M_{uf} = 0.45f_{cu} (b - b_w) h_f (d - 0.5h_f)$				N/A	kNm
2	$K_f = \frac{M - M_{uf}}{f_{cu} b_w d^2}$				N/A	
2	Ratio, K'				N/A	
2	$\beta_b$	$K' =$	0.156 for $f_{cu} \leq 60$ N/mm <sup>2</sup>	N/A	mm	3.4.4.4 BC
2	0.90		0.120 for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup>	N/A	mm	3.4.4.4 BC
2	1.10		0.094 for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup>	N/A	mm	3.4.4.4 BC
2			[ $\beta_b = 1.0$ ]			
<b>If <math>K_f &lt; K' \rightarrow</math> no compression steel</b>				N/A		
$A_s = \frac{M + k_1 f_{cu} b_w d (k_2 d - h_f)}{0.95 f_y (d - 0.5h_f)}$ , $f_y \leq 460$ N/mm <sup>2</sup>				N/A	mm <sup>2</sup>	Foreword cl.3.4.4.5 BC
$k_1 =$		0.1 for $f_{cu} \leq 60$ N/mm <sup>2</sup> , 0.072 for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup> and 0.054 for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup> ; and		$k_2 =$		0.45 for $f_{cu} \leq 60$ N/mm <sup>2</sup> , 0.32 for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup> and 0.24 for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup>
2	Back-analysis of $x$ in $(0.67f_{cu}/1.5) \cdot [b \cdot h_f + (s - h_f) \cdot b_w] = (f_y/1.05) \cdot (A_s - A_s')$				N/A	mm
2	$s =$				N/A	mm
2	0.9x for $f_{cu} \leq 60$ N/mm <sup>2</sup> ; 0.8x for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup> 0.72x for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup>				$x_{limit} = 0.5d$	mm
2	Note for an under reinforced section, require $x \leq x_{limit}$ for yielding of tension steel;					
<b>If <math>K_f &gt; K' \rightarrow</math> compression steel required</b>				N/A		
Compression steel, $A_s' = [M - (K' f_{cu} b_w d^2 + M_{uf})] / [0.95 f_y (d - d')]$ , $f_y \leq 460$				N/A	mm <sup>2</sup>	Foreword
Tension steel, $A_s = [\{0.20, 0.18, 0.16\} f_{cu} b_w d + 0.45 f_{cu} h_f (b - b_w)] / (0.95 f_y)$				N/A	mm <sup>2</sup>	Foreword
Note the coefficient 0.20, 0.18 or 0.16 is used for $f_{cu} \leq 60, 75$ or $105$ N/mm <sup>2</sup> respectively;						
If $d' > \left(1 - \frac{f_y}{735}\right) x$ , use $700 \left(1 - \frac{d'}{x}\right)$ in lieu of $0.95 f_y$				$x = 0.5d$	$f_y \leq 460$	N/A
Back-analysis of $x$ in $(0.67f_{cu}/1.5) \cdot [b \cdot h_f + (s - h_f) \cdot b_w] + (f_y/1.05) \cdot (A_s - A_s')$				N/A	mm	N/A
2	$s =$				N/A	mm
2	0.9x for $f_{cu} \leq 60$ N/mm <sup>2</sup> ; 0.8x for $60 < f_{cu} \leq 75$ N/mm <sup>2</sup> 0.72x for $75 < f_{cu} \leq 105$ N/mm <sup>2</sup>				N/A	mm
2	Note for an under reinforced section, require $\epsilon_{st} = \epsilon_{cc} (d - x) / x \geq \epsilon_y$ for yielding of tension steel					
and $\epsilon_{sc} = \epsilon_{cc} (x - d') / x \geq \epsilon_y$ for yielding of compression steel, where $\epsilon_{cc} = 0.0035$ for $f_{cu} \leq 60$ N/mm <sup>2</sup> and $\epsilon_{cc} = 0.0035 - (f_{cu} - 60) / 50000$ for $f_{cu} > 60$ N/mm <sup>2</sup> and $\epsilon_y = (f_y / 1.05) / E_s$ ;						



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<b>Shear Rectangular Beam (BS8110)</b>																																																																																																
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>																																																																																																
<i>Note that d is the effective depth to the tension reinforcement irrespective of whether the section is sagging at midspans or hogging at supports. It follows then, for midspans, tension steel is the bottom steel whilst for supports, tension steel is the top steel;</i>																																																																																																
2																																																																																																
Ultimate shear stress, $v_{ult} = V_d/b_w d$ ( $< 0.8f_{cu}^{0.5}$ & $\{5.0, 7.0\}$ N/mm <sup>2</sup> )					2.55	N/mm <sup>2</sup>	3.4.5.2 BC																																																																																									
Ultimate shear strength, $\text{MIN}\{0.8f_{cu}^{0.5}$ & $\{5.0, 7.0\}$ N/mm <sup>2</sup>					4.73	N/mm <sup>2</sup>	3.4.5.2 BC																																																																																									
Ultimate shear stress utilisation					54%		OK																																																																																									
Design shear stress, $v_d = V_d/b_w d$					2.55	N/mm <sup>2</sup>																																																																																										
Enhanced shear strength, $2d/a_v \cdot v_c$ ( $< 0.8f_{cu}^{0.5}$ & $\{5.0, 7.0\}$ N/mm <sup>2</sup> $\times 1.00$ )					0.79	N/mm <sup>2</sup>	cl.3.4.5.8																																																																																									
Distance, $a_v$					2.00d	1834	mm																																																																																									
<i>(Shear capacity enhancement by calculating <math>v_d</math> within 2d of support and comparing against enhanced <math>v_c</math> within 2d of the support as clause 3.4.5.8 BS8110 employed instead of calculating <math>v_d</math> at d from support and comparing against unenhanced <math>v_c</math> as clause 3.4.5.10 BS8110;)</i>							Note																																																																																									
Area of tension steel reinforcement provided, $A_{s,prov}$					6434	mm <sup>2</sup>																																																																																										
$\rho_w = 100A_{s,prov}/b_w d$					1.40	%																																																																																										
$v_c = (0.79/1.25)(\rho_w f_{cu}/25)^{1/3}(400/d)^{1/4}$					0.79	N/mm <sup>2</sup>	cl.3.4.5.4																																																																																									
$\rho_w = 100A_{s,prov}/b_w d \leq 3$					1.40	%	cl.3.4.5.4																																																																																									
$f_{cu} = f_{cu} \leq 80$ N/mm <sup>2</sup>					35	N/mm <sup>2</sup>	3.4.5.4 BC																																																																																									
$(400/d)^{1/4} \geq (0.67 \text{ or } 1.00)$					1.00		cl.3.4.5.4																																																																																									
<table border="1"> <caption>Table 3.8 — Values of <math>v_c</math> design concrete shear stress</caption> <thead> <tr> <th rowspan="2"><math>\frac{100A_s}{b_w d}</math></th> <th colspan="8">Effective depth (mm)</th> </tr> <tr> <th>125</th> <th>150</th> <th>175</th> <th>200</th> <th>225</th> <th>250</th> <th>300</th> <th>400</th> </tr> </thead> <tbody> <tr> <td><math>\leq 0.15</math></td> <td>0.45</td> <td>0.43</td> <td>0.41</td> <td>0.40</td> <td>0.39</td> <td>0.38</td> <td>0.36</td> <td>0.34</td> </tr> <tr> <td>0.25</td> <td>0.53</td> <td>0.51</td> <td>0.49</td> <td>0.47</td> <td>0.46</td> <td>0.45</td> <td>0.43</td> <td>0.40</td> </tr> <tr> <td>0.50</td> <td>0.67</td> <td>0.64</td> <td>0.62</td> <td>0.60</td> <td>0.58</td> <td>0.56</td> <td>0.54</td> <td>0.50</td> </tr> <tr> <td>0.75</td> <td>0.77</td> <td>0.73</td> <td>0.71</td> <td>0.68</td> <td>0.66</td> <td>0.65</td> <td>0.62</td> <td>0.57</td> </tr> <tr> <td>1.00</td> <td>0.84</td> <td>0.81</td> <td>0.78</td> <td>0.75</td> <td>0.73</td> <td>0.71</td> <td>0.68</td> <td>0.63</td> </tr> <tr> <td>1.50</td> <td>0.97</td> <td>0.92</td> <td>0.89</td> <td>0.86</td> <td>0.83</td> <td>0.81</td> <td>0.78</td> <td>0.72</td> </tr> <tr> <td>2.00</td> <td>1.06</td> <td>1.02</td> <td>0.98</td> <td>0.95</td> <td>0.92</td> <td>0.89</td> <td>0.86</td> <td>0.80</td> </tr> <tr> <td><math>\geq 3.00</math></td> <td>1.22</td> <td>1.16</td> <td>1.12</td> <td>1.08</td> <td>1.05</td> <td>1.02</td> <td>0.98</td> <td>0.91</td> </tr> </tbody> </table> <p>NOTE 1 Allowance has been made in these figures for a <math>v_m</math> of 1.25.</p> <p>NOTE 2 The values in the table are derived from the expression:  <math>0.79(100A_s/b_w d)^{1/3}(400/d)^{1/4}/v_m</math>  where  <math>\frac{100A_s}{b_w d}</math> should not be taken as greater than 3.  <math>(\frac{400}{d})^{1/4}</math> should not be taken as less than 0.67 for members without shear reinforcement.  <math>(\frac{400}{d})^{1/4}</math> should not be taken as less than 1 for members with shear reinforcement providing a design shear resistance of <math>\geq 0.4</math> N/mm<sup>2</sup>.</p> <p>For characteristic concrete strengths greater than 25 N/mm<sup>2</sup> the values in this table may be multiplied by <math>(f_{cu}/25)^{1/3}</math>. The value of <math>f_{cu}</math> should not be taken as greater than 40.</p>								$\frac{100A_s}{b_w d}$	Effective depth (mm)								125	150	175	200	225	250	300	400	$\leq 0.15$	0.45	0.43	0.41	0.40	0.39	0.38	0.36	0.34	0.25	0.53	0.51	0.49	0.47	0.46	0.45	0.43	0.40	0.50	0.67	0.64	0.62	0.60	0.58	0.56	0.54	0.50	0.75	0.77	0.73	0.71	0.68	0.66	0.65	0.62	0.57	1.00	0.84	0.81	0.78	0.75	0.73	0.71	0.68	0.63	1.50	0.97	0.92	0.89	0.86	0.83	0.81	0.78	0.72	2.00	1.06	1.02	0.98	0.95	0.92	0.89	0.86	0.80	$\geq 3.00$	1.22	1.16	1.12	1.08	1.05	1.02	0.98	0.91
$\frac{100A_s}{b_w d}$	Effective depth (mm)																																																																																															
	125	150	175	200	225	250	300	400																																																																																								
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1.50	0.97	0.92	0.89	0.86	0.83	0.81	0.78	0.72																																																																																								
2.00	1.06	1.02	0.98	0.95	0.92	0.89	0.86	0.80																																																																																								
$\geq 3.00$	1.22	1.16	1.12	1.08	1.05	1.02	0.98	0.91																																																																																								
Minimum shear strength, $v_r = \text{MAX}(0.4, 0.4(f_{cu}/40)^{2/3})$ , $f_{cu} \leq 80$ N/mm <sup>2</sup>					0.40	N/mm <sup>2</sup>	3.4.5.3 BC																																																																																									
<b>Check <math>v_d &lt; 0.5 \cdot 2d/a_v \cdot v_c</math> for no links (minor elements)</b>					INVALID	0.40	cl.3.4.5.3																																																																																									
Concrete shear capacity $2d/a_v \cdot v_c \cdot (b_w d)$					363	kN	4.5.4, cl.3.4																																																																																									
<b>Check <math>0.0 &lt; v_d &lt; v_r + 2d/a_v \cdot v_c</math> for nominal links</b>					0.00	N/A	1.19																																																																																									
$(A_{sv}/S)_{nom} > v_r \cdot b_w / (0.95f_{yv})$ , $f_{yv} \leq 460$ N/mm <sup>2</sup> i.e. $(A_{sv}/S)_{nom} >$					0.46	mm <sup>2</sup> /mm	4.5.3, cl.3.4																																																																																									
$V_{cap,nom} = (v_r + 2d/a_v \cdot v_c) \cdot (b_w d)$					546	kN	4.5.3, cl.3.4																																																																																									
<b>Check <math>v_d &gt; v_r + 2d/a_v \cdot v_c</math> for design links</b>					1.19	VALID	4.73																																																																																									
$A_{sv}/S > b_w(v_d - 2d/a_v \cdot v_c) / (0.95f_{yv})$ , $f_{yv} \leq 460$ N/mm <sup>2</sup> i.e. $A_{sv}/S >$					2.01	mm <sup>2</sup> /mm	cl.3.4.5.8,																																																																																									
$V_{cap} = (A_{sv,prov}/S + A_{sv,prov,t}/S_t) \cdot (0.95f_{yv}) \cdot d + 2d/a_v \cdot v_c \cdot (b_w d)$ , $f_{yv} \leq 460$					1622	kN	cl.3.4.5.8,																																																																																									
Area prov. by all shear and torsion links in section, $A_{sv,prov} + A_{sv,prov,t}$					314	mm <sup>2</sup>																																																																																										
Tried $A_{sv,prov}/S + A_{sv,prov,t}/S_t$ value					3.14	mm <sup>2</sup> /mm																																																																																										
Design shear resistance utilisation					72%		OK																																																																																									
<i>Note while minimum links should be provided in all beams of structural importance, it may be satisfactory to omit them in members of minor structural importance such as lintels or where the maximum design shear stress is less than half <math>2d/a_v \cdot v_c</math>;</i>																																																																																																

CONSULTING ENGINEERS		Engineering Calculation Sheet Consulting Engineers			Job No.	Sheet No.	Rev.																																																																																																			
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Job Title	Member Design - Reinforced Concrete Beam BS8110,			Drg. Ref.																																																																																																						
Member Design - RC Beam				Made by	XX	Date	16/1/2024																																																																																																			
							Chd.																																																																																																			
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<b>Shear Rectangular Beam (EC2)</b>																																																																																																										
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>																																																																																																										
<i>Note that d is the effective depth to the tension reinforcement irrespective of whether the section is sagging at midspans or hogging at supports. It follows then, for midspans, tension steel is the bottom steel whilst for supports, tension steel is the top steel;</i>																																																																																																										
Ultimate shear stress, $v_{ult} = V_d/b_w d$ ( $< v_{Rd,max(\theta=45^\circ)}=0.18(1-f_{ck}/250).f_{ck}$ , $f_{ck} \leq 50$ )				2.55	N/mm <sup>2</sup>	3(3), cl.3.1																																																																																																				
Ultimate shear strength, $v_{Rd,max(\theta=45^\circ)}=0.18(1-f_{ck}/250).f_{ck}$ , $f_{ck} \leq 50$ N/mm <sup>2</sup>				4.48	N/mm <sup>2</sup>	3(3), cl.3.1																																																																																																				
Ultimate shear stress utilisation				57%		OK																																																																																																				
Design shear stress, $v_d = V_d/b_w d$				2.55	N/mm <sup>2</sup>																																																																																																					
Enhanced shear strength, $2d/a_v \cdot v_{Rd,c}$ ( $< v_{Rd,max(\theta=45^\circ)}=0.18(1-f_{ck}/250).f_{ck}$ , $f_{ck} \leq 50$ ) $\times 1.00$				0.60	N/mm <sup>2</sup>	cl.6.2.3(8)																																																																																																				
Distance, $a_v$				2.00d	1834	mm																																																																																																				
<i>(Shear capacity enhancement by calculating <math>v_d</math> within 2d of support and comparing against enhanced <math>v_{Rd,c}</math> within 2d of the support as clause 6.2.2(6) EC2 employed instead of calculating <math>v_d</math> at d from support and comparing against unenhanced <math>v_{Rd,c}</math>)</i>				<b>Note</b>																																																																																																						
Area of tension steel reinforcement provided, $A_{s,prov}$				6434	mm <sup>2</sup>																																																																																																					
$\rho_w = 100A_{s,prov}/b_w d$				1.40	%																																																																																																					
$v_{Rd,c} = C_{Rd,c} \cdot k(\rho_w f_{ck})^{1/3} + k_1 \cdot \sigma_{cp} \geq v_{min} + k_1 \cdot \sigma_{cp}$ ; $v_{min} = 0.035k^{3/2} f_{ck}^{0.5}$ , $k = 1 + \sqrt{200/d} \leq 2.0$				0.60	N/mm <sup>2</sup>	2(1), cl.3.1																																																																																																				
$C_{Rd,c} = 0.18/\gamma_c = 0.18/1.5 = 0.12$				0.12		cl.6.2.2(1)																																																																																																				
$k = 1 + \sqrt{(200/d)} \leq 2.0$				1.47		cl.6.2.2(1)																																																																																																				
$\rho_w = 100A_{s,prov}/b_w d \leq 2$				1.40	%	cl.6.2.2(1)																																																																																																				
$\sigma_{cp} = F/b_w h \leq 0.2f_{cd} = 0.2\alpha_{cc} \cdot f_{ck}/\gamma_c = 0.2(1.0 \cdot f_{ck}/1.5)$ , $f_{ck} \leq 50$				0.00	N/mm <sup>2</sup>	2(1), cl.3.1																																																																																																				
<table border="1"> <caption>Table 8.2 Shear resistance of slabs without shear reinforcement <math>v_{Rd,c}</math> N/mm<sup>2</sup> (Class C30/37 concrete)</caption> <thead> <tr> <th rowspan="2"><math>\rho_1 = A_s/bd</math></th> <th colspan="9">Effective depth, d (mm)</th> </tr> <tr> <th><math>\leq 200</math></th> <th>225</th> <th>250</th> <th>300</th> <th>350</th> <th>400</th> <th>500</th> <th>600</th> <th>750</th> </tr> </thead> <tbody> <tr> <td>0.25%</td> <td>0.54</td> <td>0.52</td> <td>0.50</td> <td>0.47</td> <td>0.45</td> <td>0.43</td> <td>0.40</td> <td>0.38</td> <td>0.36</td> </tr> <tr> <td>0.50%</td> <td>0.59</td> <td>0.57</td> <td>0.56</td> <td>0.54</td> <td>0.52</td> <td>0.51</td> <td>0.48</td> <td>0.47</td> <td>0.45</td> </tr> <tr> <td>0.75%</td> <td>0.68</td> <td>0.66</td> <td>0.64</td> <td>0.62</td> <td>0.59</td> <td>0.58</td> <td>0.55</td> <td>0.53</td> <td>0.51</td> </tr> <tr> <td>1.00%</td> <td>0.75</td> <td>0.72</td> <td>0.71</td> <td>0.68</td> <td>0.65</td> <td>0.64</td> <td>0.61</td> <td>0.59</td> <td>0.57</td> </tr> <tr> <td>1.25%</td> <td>0.80</td> <td>0.78</td> <td>0.76</td> <td>0.73</td> <td>0.71</td> <td>0.69</td> <td>0.66</td> <td>0.63</td> <td>0.61</td> </tr> <tr> <td>1.50%</td> <td>0.85</td> <td>0.83</td> <td>0.81</td> <td>0.78</td> <td>0.75</td> <td>0.73</td> <td>0.70</td> <td>0.67</td> <td>0.65</td> </tr> <tr> <td>2.00%</td> <td>0.94</td> <td>0.91</td> <td>0.89</td> <td>0.85</td> <td>0.82</td> <td>0.80</td> <td>0.77</td> <td>0.74</td> <td>0.71</td> </tr> <tr> <td>k</td> <td>2.000</td> <td>1.943</td> <td>1.894</td> <td>1.816</td> <td>1.756</td> <td>1.707</td> <td>1.632</td> <td>1.577</td> <td>1.516</td> </tr> </tbody> </table>								$\rho_1 = A_s/bd$	Effective depth, d (mm)									$\leq 200$	225	250	300	350	400	500	600	750	0.25%	0.54	0.52	0.50	0.47	0.45	0.43	0.40	0.38	0.36	0.50%	0.59	0.57	0.56	0.54	0.52	0.51	0.48	0.47	0.45	0.75%	0.68	0.66	0.64	0.62	0.59	0.58	0.55	0.53	0.51	1.00%	0.75	0.72	0.71	0.68	0.65	0.64	0.61	0.59	0.57	1.25%	0.80	0.78	0.76	0.73	0.71	0.69	0.66	0.63	0.61	1.50%	0.85	0.83	0.81	0.78	0.75	0.73	0.70	0.67	0.65	2.00%	0.94	0.91	0.89	0.85	0.82	0.80	0.77	0.74	0.71	k	2.000	1.943	1.894	1.816	1.756	1.707	1.632	1.577	1.516
$\rho_1 = A_s/bd$	Effective depth, d (mm)																																																																																																									
	$\leq 200$	225	250	300	350	400	500	600	750																																																																																																	
0.25%	0.54	0.52	0.50	0.47	0.45	0.43	0.40	0.38	0.36																																																																																																	
0.50%	0.59	0.57	0.56	0.54	0.52	0.51	0.48	0.47	0.45																																																																																																	
0.75%	0.68	0.66	0.64	0.62	0.59	0.58	0.55	0.53	0.51																																																																																																	
1.00%	0.75	0.72	0.71	0.68	0.65	0.64	0.61	0.59	0.57																																																																																																	
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k	2.000	1.943	1.894	1.816	1.756	1.707	1.632	1.577	1.516																																																																																																	
Minimum shear strength, $v_r = 0.08/\gamma_s \cdot f_{ck}^{0.5}$ , $\gamma_s = 1.15$ , $f_{ck} \leq 50$ N/mm <sup>2</sup>				0.37	N/mm <sup>2</sup>	2(5), cl.3.1																																																																																																				
<b>Check <math>v_d &lt; 2d/a_v \cdot v_{Rd,c}</math> for no links (minor elements)</b>				INVALID	0.60	cl.6.2.1(3)																																																																																																				
4.5.8	Concrete shear capacity $2d/a_v \cdot v_{Rd,c} \cdot (b_w d)$			274	kN	2(1), cl.6.2.3(8)																																																																																																				
<b>Check <math>0.0 &lt; v_d &lt; v_r</math> for nominal links</b>				0.00	N/A	0.37	cl.6.2.1(5)																																																																																																			
4.5.1	$(A_{sv}/S)_{nom} > v_r \cdot b_w / (0.87f_{yv})$ , $f_{yv} \leq 600$ N/mm <sup>2</sup> i.e. $(A_{sv}/S)_{nom} >$			0.42	mm <sup>2</sup> /mm	3(3), cl.3.1																																																																																																				
4.5.8	$V_{cap,nom} = 2d/a_v \cdot (A_{sv}/S)_{nom} \cdot (0.87f_{yv}) \cdot 0.9d \cdot \cot\theta$ , $f_{yv} \leq 600$ N/mm <sup>2</sup>			376	kN	cl.6.2.3(8)																																																																																																				
<b>Check <math>v_d &gt; v_r</math> for design links</b>				0.37	VALID	4.48	cl.6.2.1(5)																																																																																																			
cl.3.4.5.1	$A_{sv}/S > b_w \cdot v_d / (0.9(0.87f_{yv}) \cdot \cot\theta) / (2d/a_v)$ , $f_{yv} \leq 600$ N/mm <sup>2</sup> i.e. $A_{sv}/S >$			1.32	mm <sup>2</sup> /mm	cl.6.2.3(8)																																																																																																				
cl.3.4.5.1	$V_{cap} = 2d/a_v \cdot (A_{sv,prov}/S + A_{sv,prov,t}/S_t) \cdot (0.87f_{yv}) \cdot 0.9d \cdot \cot\theta$ , $f_{yv} \leq 600$ N/mm <sup>2</sup>			2792	kN	cl.6.2.3(8)																																																																																																				
Comp. strut angle, $\theta = 22^\circ \leq 0.5 \sin^{-1}\{v_d/v_{Rd,max(\theta=45^\circ)}\} \leq 45^\circ$				22.0	°	cl.6.2.3(2)																																																																																																				
Area prov. by all shear and torsion links in section, $A_{sv,prov} + A_{sv,prov,t}$				314	mm <sup>2</sup>																																																																																																					
Tried $A_{sv,prov}/S + A_{sv,prov,t}/S_t$ value				3.14	mm <sup>2</sup> /mm																																																																																																					
Design shear resistance utilisation				42%		OK																																																																																																				
<i>Note while minimum links should be provided in all beams of structural importance, it may be satisfactory to omit them in members of minor structural importance such as lintels or where the maximum design shear stress is less than <math>2d/a_v \cdot v_{Rd,c}</math>;</i>																																																																																																										

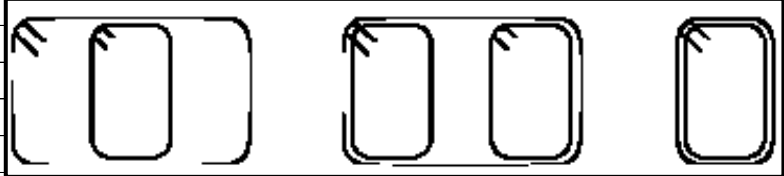
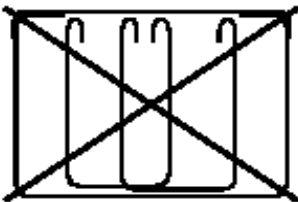
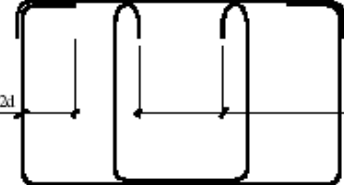
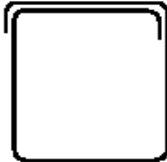
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					Member/Location												
Job Title	Member Design - Reinforced Concrete Beam BS8110,				Drg. Ref.												
Member Design - RC Beam					Made by	XX	Date										
						16/1/2024	Chd.										
							ACI318										
<b>Shear Rectangular Beam (ACI318)</b>																	
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>																	
<i>Note that d is the effective depth to the tension reinforcement irrespective of whether the section is sagging at midspans or hogging at supports. It follows then, for midspans, tension steel is the bottom steel whilst for supports, tension steel is the top steel;</i>																	
Ultimate shear stress, $v_{ult} = V_d^*/b_wd$ ( $< \phi(0.66+0.17\lambda)\sqrt{f_c'}$ , $f_c' \leq 70N/mm^2$ )					2.55	N/mm <sup>2</sup>	cl.22.5.5.1										
Ultimate shear strength, $\phi(0.66+0.17\lambda)\sqrt{f_c'}$ , $f_c' \leq 70N/mm^2$					3.29	N/mm <sup>2</sup>	cl.22.5.5.1										
Ultimate shear stress utilisation					77%		OK										
Design shear stress, $v_d = V_d^*/b_wd$					2.55	N/mm <sup>2</sup>											
Enhanced shear strength, $d/a_v.v_c$					x 1.00	0.67	N/mm <sup>2</sup> cl.9.4.3.2										
Distance, $a_v$					2.00d	1834	mm										
<i>(Shear capacity enhancement by calculating <math>v_d</math> within d of support and comparing against enhanced <math>v_c</math> within d of the support employed instead of calculating <math>v_d</math> at d from support and comparing against unenhanced <math>v_c</math> as clause 9.4.3.2 ACI318);</i>							Note										
Area of tension steel reinforcement provided, $A_{s,prov}$					6434	mm <sup>2</sup>											
$\rho_w = 100A_{s,prov}/b_wd$					1.40	%											
9.2(2) $v_c = \phi V_d/b_wd$ Note $f_c' \leq 70N/mm^2$ Simplified					0.67	N/mm <sup>2</sup>											
$V_c = 0.17\lambda\sqrt{f_c'}b_wd$					[Simplified] $\phi V_c =$	309	kN 5.5.1, cl.22										
9.2(2) where $\lambda = \{1.00 \text{ NWC}, 0.75 \text{ LWC}\}$ Normal weight																	
<b>Table 22.5.5.1—Detailed method for calculating <math>V_c</math></b>																	
<table border="1"> <tr> <td colspan="2"><math>V_c</math></td> <td></td> </tr> <tr> <td rowspan="3">Least of (a), (b), and (c):</td> <td><math>\left(0.16\lambda\sqrt{f_c'} + 17\rho_w \frac{V_u d}{M_u}\right) b_w d</math> <sup>(1)</sup></td> <td>(a)</td> </tr> <tr> <td><math>(0.16\lambda\sqrt{f_c'} + 17\rho_w) b_w d</math></td> <td>(b)</td> </tr> <tr> <td><math>0.29\lambda\sqrt{f_c'} b_w d</math></td> <td>(c)</td> </tr> </table>								$V_c$			Least of (a), (b), and (c):	$\left(0.16\lambda\sqrt{f_c'} + 17\rho_w \frac{V_u d}{M_u}\right) b_w d$ <sup>(1)</sup>	(a)	$(0.16\lambda\sqrt{f_c'} + 17\rho_w) b_w d$	(b)	$0.29\lambda\sqrt{f_c'} b_w d$	(c)
$V_c$																	
Least of (a), (b), and (c):	$\left(0.16\lambda\sqrt{f_c'} + 17\rho_w \frac{V_u d}{M_u}\right) b_w d$ <sup>(1)</sup>	(a)															
	$(0.16\lambda\sqrt{f_c'} + 17\rho_w) b_w d$	(b)															
	$0.29\lambda\sqrt{f_c'} b_w d$	(c)															
<sup>(1)</sup> $M_u$ occurs simultaneously with $V_u$ at the section considered.																	
where $\lambda = \{1.00 \text{ NWC}, 0.75 \text{ LWC}\}$ Normal weight																	
Strength reduction factor for shear, $\phi = 0.75$					0.75		cl.21.2										
Minimum shear strength, $v_r = \text{MAX}(0.35, 0.062\sqrt{f_c'})$ , $f_c' \leq 70N/mm^2$					0.35	N/mm <sup>2</sup>	5.2.2, cl.22										
<b>Check <math>v_d &lt; 0.5.d/a_v.v_c</math> for no links (minor elements)</b>					INVALID	0.34	cl.9.6.3.1										
9.2(6) Concrete shear capacity $d/a_v.v_c.(b_wd)$					309	kN	5.5.1, cl.9.										
<b>Check <math>0.0 &lt; v_d &lt; \phi v_r + d/a_v.v_c</math> for nominal links</b>					0.00	N/A	0.94 cl.9.6.3.1										
9.2(3) $(A_{sv}/S)_{nom} > v_r.b_w/f_{yv}$ , $f_{yv} \leq 420N/mm^2$ i.e. $(A_{sv}/S)_{nom} >$					0.42	mm <sup>2</sup> /mm	5.10.5, cl.2										
cl.3.2.2(3) $V_{cap,nom} = (\phi d/a_v.v_r + d/a_v.v_c).(b_wd)$					430	kN	5.10.5.3, cl.										
<b>Check <math>v_d &gt; \phi v_r + d/a_v.v_c</math> for design links</b>					0.94	VALID	3.29 cl.22.5.10.1										
cl.3.2.2(3) $A_{sv}/S > b_w(v_d - d/a_v.v_c)/(\phi f_{yv})/(d/a_v)$ , $f_{yv} \leq 420N/mm^2$ i.e. $A_{sv}/S >$					2.98	mm <sup>2</sup> /mm	5, cl.9.4.3.2										
cl.3.2.2(3) $V_{cap} = \phi d/a_v.(A_{sv,prov}/S + A_{sv,prov,t}/S_t).f_{yv}.d + d/a_v.v_c.(b_wd)$ , $f_{yv} \leq 420N$					1217	kN	5.10.5.3, cl.										
Area prov. by all shear and torsion links in section, $A_{sv,prov} + A_{sv,prov,t}$					314	mm <sup>2</sup>											
Tried $A_{sv,prov}/S + A_{sv,prov,t}/S_t$ value					3.14	mm <sup>2</sup> /mm											
Design shear resistance utilisation					96%		OK										
<i>Note while minimum links should be provided in all beams of structural importance, it may be satisfactory to omit them in members of minor structural importance such as lintels or where the maximum design shear stress is less than half <math>d/a_v.v_c</math>;</i>																	

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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								BS8110-2	
<b>Torsion Rectangular Beam (BS8110)</b>									
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>									
Larger dimension of rectangular section, $h_{max} = \text{MAX}(h, b_w)$					1000	mm			
Smaller dimension of rectangular section, $h_{min} = \text{MIN}(h, b_w)$					500	mm			
Design torsion moment, T					0	kNm			
Design torsion stress, $v_t = 2T/((h_{min}^2)(h_{max}-h_{min}/3)) (< 0.8f_{cu}^{0.5} \& \{5.0,7.0\}N/mm^2)$					0.00	N/mm <sup>2</sup>	cl.2.4.4.1		
Ultimate torsion strength, $\text{MIN}\{0.8f_{cu}^{0.5} \& \{5.0,7.0\}N/mm^2\}$					4.73	N/mm <sup>2</sup>	3.4.5.2 BC		
Design ultimate torsion stress utilisation					0%		OK		
<b>Check <math>v_t &lt; v_{t.min}</math> for no torsion links</b>					VALID		cl.2.4.6		
Concrete torsion resistance, $v_{t.min} = \text{MIN}(0.6, 0.067\sqrt{f_{cu}}), f_{cu} \leq 80$					0.40	N/mm <sup>2</sup>	cl.2.3 BC2		
<b>Check <math>v_t &gt; v_{t.min}</math> for design torsion links</b>					N/A		cl.2.4.6		
Horizontal dimension of closed link, $x_1 = b_w - 2 \times \text{cover} - \phi_{link,t}$					450	mm			
Vertical dimension of closed link, $y_1 = h - 2 \times \text{cover} - \phi_{link,t}$					950	mm			
Provide torsion links $A_{sv,t}/S_t > T/(0.8x_1y_1(0.95f_{yv}))$ , $f_{yv} \leq 460N/mm^2$					0.00	mm <sup>2</sup> /mm	4.7, Forew		
Provide torsion longitudinal bars, $A_{s,t}$					0	mm <sup>2</sup>	4.7, Forew		
<i>Note require <math>A_{s,t} &gt; (A_{sv,t}/S_t)(f_{yv}/f_y)(x_1+y_1)</math>, <math>f_y \leq 460N/mm^2</math>, <math>f_{yv} \leq 460N/mm^2</math>; cl.2.4.7, Forew</i>									
Area provided by all torsion links in a cross-section, $A_{sv,prov,t}$					0	mm <sup>2</sup>			
Tried $A_{sv,prov,t}/S_t$ value					0.00	mm <sup>2</sup> /mm			
Design torsion resistance utilisation					0%		OK		
<b>Combined Shear and Torsion Rectangular Beam (BS8110)</b>									
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>									
5.3.1									
Ultimate shear and torsion stresses $v_{ult} + v_t (< 0.8f_{cu}^{0.5} \& \{5.0,7.0\}N/mm^2)$					2.55	N/mm <sup>2</sup>	cl.2.4.5		
Ultimate shear and torsion strength, $\text{MIN}\{0.8f_{cu}^{0.5} \& \{5.0,7.0\}N/mm^2\}$					4.73	N/mm <sup>2</sup>	3.4.5.2 BC		
Ultimate shear and torsion stresses utilisation					54%		OK		
5.3.1									
<b>Check design shear and torsion links</b>									
Provide single torsion link leg $> A_{sv}/S/(n_{leg}+n_{leg,t}) + A_{sv,t}/S_t/n_{leg,t}$					0.34	mm <sup>2</sup> /mm			
Area provided by single torsion link leg, $A_{sv,prov,t}/n_{leg,t}$					0	mm <sup>2</sup>			
Tried $A_{sv,prov,t}/n_{leg,t}/S_t$ value					0.00	mm <sup>2</sup> /mm			
Design shear and torsion resistance utilisation					0%		OK		
4.3.2									
2.5.3.3									
9.4.3.2, cl.22.5.3.3									
, cl.22.5.3.3									
9.4.3.2, cl.22.5.3.3									



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			jXXX	17		
			Member/Location			
Job Title	Member Design - Reinforced Concrete Beam BS8110,	Drg. Ref.				
Member Design - RC Beam		Made by	XX	Date	16/1/2024	
					Chd.	
					EC2	
<b>Torsion Rectangular Beam (EC2)</b>						
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>						
Larger dimension of rectangular section, $h_{max} = \text{MAX}(h, b_w)$			1000	mm		
Smaller dimension of rectangular section, $h_{min} = \text{MIN}(h, b_w)$			500	mm		
Design torsion moment, $T_d$			0	kNm		
Design torsion stress, $v_t = T_d/(t_{ef} \cdot 2A_k)$			0.00	N/mm <sup>2</sup>	MOSLEY	
Ultimate torsion moment capacity, $T_{Rd,max(\theta=45^\circ)} = 1.33v_{1,fc} \cdot t_{ef} \cdot A_k / (\cot\theta + \tan\theta)$ ,			459	kNm	2(4), cl.3.	
Design ultimate torsion moment capacity utilisation			0%		OK	
<b>Check <math>T_d &lt; T_{Rd,c}</math> for no torsion links</b>			<b>VALID</b>			
Concrete torsion resistance, $T_{Rd,c} = f_{ctd} \cdot t_{ef} \cdot 2A_k, f_{ck} \leq 50\text{N/mm}^2$			120	kNm		
where $f_{ctd} = \alpha_{ct} \cdot f_{ctk} / \gamma_{cr}$ $\alpha_{ct} = 1.0, \gamma_{cr} = 1.5, f_{ctk} = 0.7f_{ctm}, f_{ctm} = 0.30f_{ck}^{2/3}$			cl.3.1.6			
<b>Check <math>T_d &gt; T_{Rd,c}</math> for design torsion links</b>			<b>N/A</b>			
Effective wall thickness, $t_{ef} = (b_w \cdot h) / [2 \cdot (b_w + h)]$			167	mm	cl.6.3.2(1)	
Area enclosed, $A_k = (b_w - t_{ef}) \cdot (h - t_{ef})$			277778	mm <sup>2</sup>	cl.6.3.2(1)	
ord	Provide torsion links $A_{sv,t}/S_t > T_d / (A_k \cdot (0.87f_{yv}) \cdot \cot\theta)$ , $f_{yv} \leq 600\text{N/mm}^2$			0.00	mm <sup>2</sup> /mm	MOSLEY
ord	Provide torsion longitudinal bars, $A_{s,t}$			0	mm <sup>2</sup>	cl.6.3.2(3)
ord	<i>Note require <math>A_{s,t} &gt; T_d \cdot u_k / (2 \cdot A_k) \cdot \cot\theta / (0.87f_y)</math>, <math>u_k = 2 \cdot (b_w + h - 2t_{ef})</math>, <math>f_y \leq 600\text{N/mm}^2</math>; cl.6.3.2(3)</i>					
Area provided by all torsion links in a cross-section, $A_{sv,prov,t}$			0	mm <sup>2</sup>		
Tried $A_{sv,prov,t}/S_t$ value			0.00	mm <sup>2</sup> /mm		
Design torsion resistance utilisation			0%		OK	
<b>Combined Shear and Torsion Rectangular Beam (EC2)</b>						
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>						
Ultimate shear and torsion $V_d/V_{Rd,max(\theta=45^\circ)} + T_d/T_{Rd,max(\theta=45^\circ)} (\leq 1.00)$			0.57		cl.6.3.2(4)	
Ultimate shear and torsion utilisation, $\leq 1.00$			1.00		cl.6.3.2(4)	
Ultimate shear and torsion utilisation			57%		OK	
<b>Check design shear and torsion links</b>						
Provide single torsion link leg $> A_{sv}/S / (n_{leg} + n_{leg,t}) + A_{sv,t}/S_t/n_{leg,t}$			0.22	mm <sup>2</sup> /mm		
Area provided by single torsion link leg, $A_{sv,prov,t}/n_{leg,t}$			0	mm <sup>2</sup>		
Tried $A_{sv,prov,t}/n_{leg,t}/S_t$ value			0.00	mm <sup>2</sup> /mm		
Design shear and torsion resistance utilisation			0%		OK	

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					jXXX	18			
Member/Location									
Job Title	Member Design - Reinforced Concrete Beam BS8110,				Drg. Ref.				
Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								ACI318	
<b>Torsion Rectangular Beam (ACI318)</b>									
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>									
Larger dimension of rectangular section, $h_{max} = \text{MAX}(h, b_w)$					1000	mm			
Smaller dimension of rectangular section, $h_{min} = \text{MIN}(h, b_w)$					500	mm			
Design torsion moment, $T^*$					0	kNm			
Design torsion stress, $v_t = T^* \cdot 2 \cdot (x_1 + y_1) / 1.7 / (x_1 y_1)^2$ ( $< \phi(0.66 + 0.17\lambda) \sqrt{f'_c}$ , $\phi = 0.75$ )					0.00	N/mm <sup>2</sup>	cl.22.7.7.1		
Ultimate torsion strength, $\phi(0.66 + 0.17\lambda) \sqrt{f'_c}$ , $\phi = 0.75$ , $f'_c \leq 70 \text{N/mm}^2$					3.29	N/mm <sup>2</sup>	cl.22.5.5.1		
Design ultimate torsion stress utilisation					0%		OK		
<b>Check <math>T &lt; \phi T_{th}</math> for no torsion links</b>					VALID				
Concrete torsion resistance, $\phi T_{th} = \phi 0.083 \lambda \sqrt{f'_c} \cdot (h_{min} \cdot h_{max})^2 / [2 \cdot (h_{min} + h_{max})]$					27	kNm	7.4.1, cl.22		
where $\lambda = \{1.00 \text{ NWC}, 0.75 \text{ LWC}\}$					Normal weight				
<b>Check <math>T &gt; \phi T_{th}</math> for design torsion links</b>					N/A				
Horizontal dimension of closed link, $x_1 = b_w - 2 \times \text{cover} - \phi_{link,t}$					450	mm			
Vertical dimension of closed link, $y_1 = h - 2 \times \text{cover} - \phi_{link,t}$					950	mm			
Provide torsion links $A_{sv,t}/S_t > T^* / (\phi 0.85 x_1 y_1 \cdot f_{yv})$ , $\phi = 0.75$ , $\theta = 40^\circ$					0.00	mm <sup>2</sup> /mm	cl.22.7.6.1		
Provide torsion longitudinal bars, $A_{s,t}$					0	mm <sup>2</sup>	7.6.1, cl.9.		
<i>Note require <math>A_{s,t} &gt; (A_{sv,t}/S_t)(f_{yv}/f_y)(x_1 + y_1) &gt; A_{l,min}</math>, <math>f_y \leq 420 \text{N/mm}^2</math>, <math>f_{yv} \leq 420 \text{N/mm}^2</math></i>									
Area provided by all torsion links in a cross-section, $A_{sv,prov,t}$					0	mm <sup>2</sup>			
Tried $A_{sv,prov,t}/S_t$ value					0.00	mm <sup>2</sup> /mm			
Design torsion resistance utilisation					0%		OK		
<b>Combined Shear and Torsion Rectangular Beam (ACI318)</b>									
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>									
Ultimate shear and torsion stresses $[v_{ult}^2 + v_t^2]^{1/2}$ ( $< \phi(0.66 + 0.17\lambda) \sqrt{f'_c}$ , $\phi = 0.75$ )					2.55	N/mm <sup>2</sup>	cl.22.7.7.1		
Ultimate shear and torsion strength, $\phi(0.66 + 0.17\lambda) \sqrt{f'_c}$ , $\phi = 0.75$ , $f'_c \leq 70 \text{N/mm}^2$					3.29	N/mm <sup>2</sup>	5.5.1, cl.22		
Ultimate shear and torsion stresses utilisation					77%		OK		
<b>Check design shear and torsion links</b>									
Provide single torsion link leg $> A_{sv}/S/(n_{leg} + n_{leg,t}) + A_{sv,t}/S/n_{leg,t}$					0.50	mm <sup>2</sup> /mm			
Provide single torsion link leg $> \text{MAX}(0.175, 0.031 \sqrt{f'_c}) \cdot b_w / f_{yv}$ , $f_{yv} \leq 420 \text{N/mm}^2$					0.21	mm <sup>2</sup> /mm	cl.9.6.4.2		
Area provided by single torsion link leg, $A_{sv,prov,t}/n_{leg,t}$					0	mm <sup>2</sup>			
Tried $A_{sv,prov,t}/n_{leg,t}/S_t$ value					0.00	mm <sup>2</sup> /mm			
Design shear and torsion resistance utilisation					0%		OK		

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				jXXX	19			
Member/Location								
Job Title	Member Design - Reinforced Concrete Beam BS8110,			Drg. Ref.				
Member Design - RC Beam				Made by	XX	Date	16/1/2024	Chd.
							BS8110	
<b>Detailing Requirements Rectangular or Flanged Beam</b>								
All detailing requirements met ?					<b>OK</b>			
Min tension steel reinforcement diameter, $\phi_t$ ( $\geq 12\text{mm}$ )				32	mm	<b>OK</b>		
Min tension steel reinforcement pitch ( $b_w - 2 \cdot \text{cover} - 2 \cdot \text{MAX}(\phi_{\text{link}}, \phi_{\text{link},t}) - \phi_t$ ) / ( $n_t/n$ )				133	mm	<b>OK</b>		
Max tension steel reinforcement pitch ( $b_w - 2 \cdot \text{cover} - 2 \cdot \text{MAX}(\phi_{\text{link}}, \phi_{\text{link},t}) - \phi_t$ ) / ( $n_t/r$ )				133	mm	<b>OK</b>		
<i>Note that max pitch assumes no moment redistribution in beam, if less than 20% moment redistribution then pitch to be less than 175mm for G250 and less than 150mm for G460;</i>								
Min compression steel reinforcement diameter, $\phi_c$ ( $\geq 12\text{mm}$ )				N/A	mm	<b>N/A</b>		
Min compression steel reinforcement pitch ( $b_w$ or $b - 2 \cdot \text{cover} - 2 \cdot \text{MAX}(\phi_{\text{link}}, \phi_{\text{link},t})$ )				N/A	mm	<b>N/A</b>		
Max compression steel reinforcement pitch ( $b_w$ or $b - 2 \cdot \text{cover} - 2 \cdot \text{MAX}(\phi_{\text{link}}, \phi_{\text{link},t})$ )				N/A	mm	<b>N/A</b>		
Min shear link diameter, $\phi_{\text{link}}$ ( $\geq 6\text{mm}$ , $\geq \phi_c/4$ )				10	mm	<b>OK</b>		
Min torsion link diameter, $\phi_{\text{link},t}$ ( $\geq 6\text{mm}$ , $\geq \phi_c/4$ )				N/A	mm	<b>N/A</b>		
Shear link pitch, $S$ ( $\leq 0.75d$ , $\leq 12\phi_c$ , $\leq 300\text{mm}$ , $\geq \text{MAX}(100\text{mm}, 50+12 \cdot \phi_c)$ )				100	mm	<b>OK</b>		
Torsion link pitch, $S_t$ ( $\leq 0.75d$ , $\leq 12\phi_c$ , $\leq 300\text{mm}$ , $\geq \text{MAX}(100\text{mm}, 50+12 \cdot \phi_c)$ )				N/A	mm	<b>N/A</b>		
$A_{sv,prov} / (b_w \cdot S) + A_{sv,prov,t} / (b_w \cdot S_t)$ ( $> 0.10\%$ G460; $> 0.17\%$ G250)				0.63	%	<b>OK</b>		
$A_{sv,prov} / (b_w \cdot S) + A_{sv,prov,t} / (b_w \cdot S_t)$ ( $< 4.00\%$ )				0.63	%	<b>OK</b>		
<i>Note require an overall enclosing link; Note require additional restraining links for each alternate longitudinal</i>								
								
A pattern which overlaps links as shown below should not be used.								
5.3.1,								
Open links may be used for beam and slab construction using 'L' hooks where the width of rib is 450mm or more. In such circumstance a top locking link is also used.								
								
Where links are used for torsion the bar shape 99 should be used to describe the shape shown below.								
								
<i>Note lacer bars of 16mm are required at the sides of beams more than 750mm deep at 250mm pitch;</i>								

BS8110

**Deflection Criteria Rectangular or Flanged Beam**

Typically require :  
 Total deflection < span/250  
 Live Load + creep < span/350  
 and < 20mm

Criterion satisfied if span / effective depth < (Basic x C<sub>1</sub> x C<sub>2</sub> x C<sub>3</sub>)

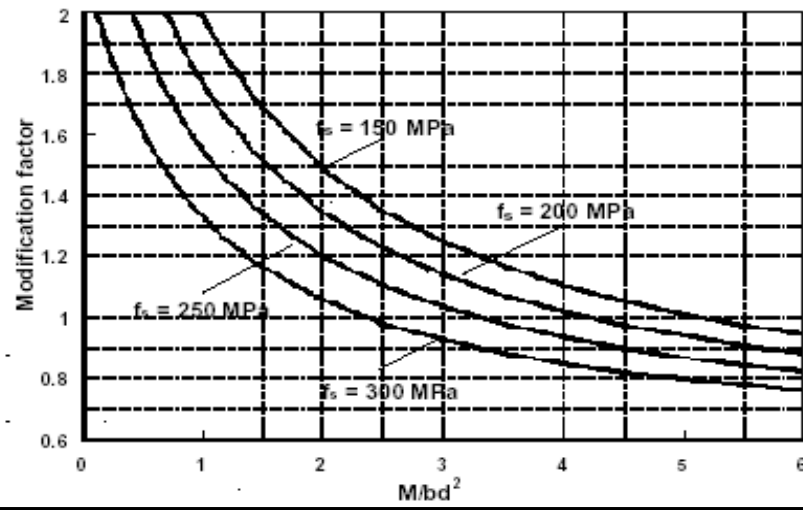
**Typical multipliers (C1):**  
 C1 = 0.8 for flanged beams with b<sub>w</sub>/b < 0.3  
 C1 = 10/span(m) for spans beyond 10m  
 C1 = 0.9 for flat slabs (use longer span)

NOTE: For two-way slabs on continuous support, use shorter span.

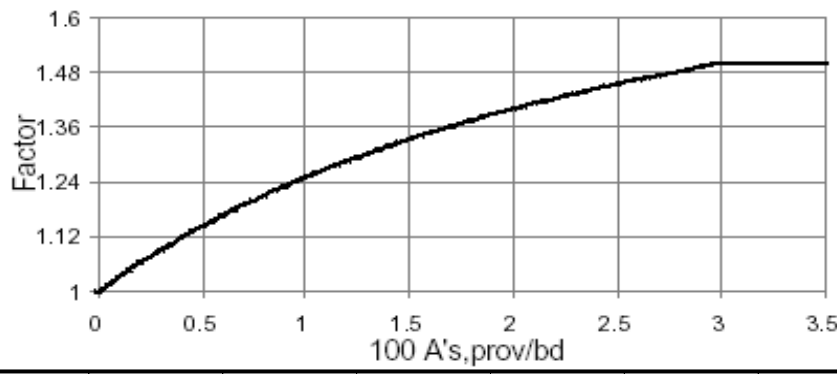
Basic span/effective depth ratios for rectangular beams	
Support conditions	Rectangular sections
Cantilever	7
Simple supported	20
Continuous	26

**Tension reinforcement modification factor (C<sub>2</sub>)<sup>4</sup>**

f<sub>s</sub> = service stress in reinforcement



**Compression reinforcement modification factor (C<sub>3</sub>)**



**Shrinkage**

For normal situations, assume long term shrinkage strain of 300 x 10<sup>-6</sup>

**Creep**

For normal situations, assume creep coefficient of φ = 2

Hence long term E value: 
$$E = \frac{E_{28}}{1 + \phi}$$

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		jXXX	21	
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Job Title	Member Design - Reinforced Concrete Beam BS8110,	Drg. Ref.		
Member Design - RC Beam		Made by	Date	Chd.
		XX	16/1/2024	
		<u>BS8110</u>		
Span			10.000 m	
Span / effective depth ratio			<b>10.9</b>	
Basic span / effective depth ratio criteria			<b>26.0</b>	
Multiplier $C_{1,rect}$ or flanged			1.00	cl.3.4.6.3
Multiplier $C_{1,span}$ more or less than 10m		Include	1.00	cl.3.4.6.4
Modification factor for tension $C_2$				
	$M/(b_w \text{ or } b).d^2$		4.40 N/mm <sup>2</sup>	cl.3.4.6.2
	$f_s = \frac{2f_y A_{s, req}}{3A_{s, prov}} \times \frac{1}{\beta_b}$		287 N/mm <sup>2</sup>	
	Modification	$0.55 + \frac{(477 - f_s)}{120 \left(0.9 + \frac{M}{bd^2}\right)} \leq 2.0$	<b>0.85</b>	T.3.10
Modification factor for compression $C_3$				
	$100A'_{s,prov}/(b_w \text{ or } b).d$		N/A	cl.3.4.6.2
	Modification	$1 + \frac{100A'_{s,prov}}{bd} / \left(3 + \frac{100A'_{s,prov}}{bd}\right) \leq 1.5$	<b>1.00</b>	T.3.11
Modified span / effective depth ratio criteria			<b>22.1</b>	
Deflection utilisation			<b>49%</b>	<b>OK</b>

**Table 3.10 — Modification factor for tension reinforcement**

Service stress	$M/bd^2$								
	0.50	0.75	1.00	1.50	2.00	3.00	4.00	5.00	6.00
100	2.00	2.00	2.00	1.86	1.63	1.36	1.19	1.08	1.01
150	2.00	2.00	1.98	1.69	1.49	1.25	1.11	1.01	0.94
( $f_y = 250$ ) 167	2.00	2.00	1.91	1.63	1.44	1.21	1.08	0.99	0.92
200	2.00	1.95	1.76	1.51	1.35	1.14	1.02	0.94	0.88
250	1.90	1.70	1.55	1.34	1.20	1.04	0.94	0.87	0.82
300	1.60	1.44	1.33	1.16	1.06	0.93	0.85	0.80	0.76
( $f_y = 460$ ) 307	1.56	1.41	1.30	1.14	1.04	0.91	0.84	0.79	0.76

NOTE 1 The values in the table derive from the equation:

$$\text{Modification factor} = 0.55 + \frac{(477 - f_s)}{120 \left(0.9 + \frac{M}{bd^2}\right)} \leq 2.0 \quad \text{equation 7}$$

where

$M$  is the design ultimate moment at the centre of the span or, for a cantilever, at the support.

NOTE 2 The design service stress in the tension reinforcement in a member may be estimated from the equation:

$$f_s = \frac{2f_y A_{s, req}}{3A_{s, prov}} \times \frac{1}{\beta_b} \quad \text{equation 8}$$

NOTE 3 For a continuous beam, if the percentage of redistribution is not known but the design ultimate moment at mid-span is obviously the same as or greater than the elastic ultimate moment, the stress  $f_s$  in this table may be taken as  $2/3f_y$ .

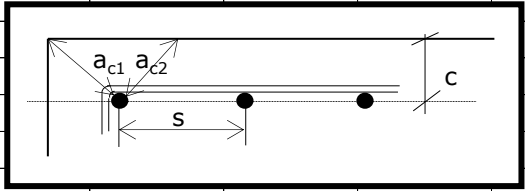
**Table 3.11 — Modification factor for compression reinforcement**

$100 \frac{A'_{s,prov}}{bd}$	Factor
0.00	1.00
0.15	1.05
0.25	1.08
0.35	1.10
0.50	1.14
0.75	1.20
1.0	1.25
1.5	1.33
2.0	1.40
2.5	1.45
$\geq 3.0$	1.50

NOTE 1 The values in this table are derived from the following equation:

$$\text{Modification factor for compression reinforcement} = 1 + \frac{100A'_{s,prov}}{bd} / \left(3 + \frac{100A'_{s,prov}}{bd}\right) \leq 1.5 \quad \text{equation 9}$$

NOTE 2 The area of compression reinforcement  $A$  used in this table may include all bars in the compression zone, even those not effectively tied with links.

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					jXXX	22			
Member/Location									
Job Title		Member Design - Reinforced Concrete Beam BS8110,			Drg. Ref.				
Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								BS8110	
<b>Crack Width Estimation Rectangular Beam</b>									
<i>Note that this design check is performed for both rectangular and flanged sections, adopting rectangular section equations in the case of flanged sections;</i>									
Maximum crack width criteria, Standard concrete BS8110 (0.30mm)					▼		0.30		mm
Load factor, LF = 1.4 conservatively							1.4		
SLS bending moment, $M_{sls} = M / LF$							1321		kNm
SLS axial force (tension +ve and compression -ve), $F_{sls} = -F / LF$							0		kN
Uncracked elastic modulus, $E_{uncracked} = 20 + 0.2f_{cu}$							27		GPa
Cracked elastic modulus, $E_{cracked} = E_{uncracked} / 2$							14		GPa
Steel elastic modulus, $E_s$							200		GPa
Modulus ratio, $\alpha_e = E_s / E_{cracked}$							14.8		
Reinforcement ratio, $\rho_w = A_{s,prov} / b_w d$							0.01		
Factor, $\alpha_e \cdot \rho_w$							0.21		
Depth of neutral axis, $x = \alpha_e \cdot \rho_w \cdot [(1 + 2 / (\alpha_e \rho_w))^{1/2} - 1] \cdot d$							431		mm
Lever arm, $z = d - x / 3$							773		mm
Steel tensile service stress (flexural), $f_{s1} = M_{sls} / z / A_{s,prov}$							265		N/mm <sup>2</sup>
Steel tensile (tensile +ve and compressive -ve) service stress (axial), $f_{s2}$							0		N/mm <sup>2</sup>
<i>Note if <math>F_{sls} &gt; 0</math>, <math>f_{s2} = F_{sls} / (A_{s,prov} + A_{s,prov}')</math>,</i>									
<i>else <math>f_{s2} = \alpha_e \cdot (A_{s,prov} + A_{s,prov}') / [\alpha_e \cdot (A_{s,prov} + A_{s,prov}') + (b_w \cdot h - A_{s,prov} - A_{s,prov}')] \cdot F_{sls} / (A_{s,prov} + A_{s,prov}')</math>;</i>									
Steel tensile service stress utilisation, $(f_{s1} + f_{s2}) / (0.8f_y) < 1.00$							66%		OK
Concrete compressive service stress (flexural and axial), $f_c$							16		N/mm <sup>2</sup>
<i>Note if <math>F_{sls} &gt; 0</math>, <math>f_c = 2(M_{sls} / z) / (b_w x)</math>, else <math>f_c = 2(M_{sls} / z) / (b_w x) + (b_w \cdot h - A_{s,prov} - A_{s,prov}') / [\alpha_e \cdot (A_{s,prov} + A_{s,prov}') + (b_w \cdot h - A_{s,prov} - A_{s,prov}')] \cdot ABS(F_{sls}) / (b_w \cdot h - A_{s,prov} + A_{s,prov}')</math>;</i>									
Concrete compressive service stress utilisation, $f_c / (0.45f_{cu}) < 1.00$							101%		NOT OK
Strain at tension face, $\epsilon_1 = (h - x) / (d - x) \cdot (f_{s1} + f_{s2}) / E_s$							1.55		x10 <sup>-3</sup>
Strain stiffening, $\epsilon_2 = b_w (h - x)^2 / [3E_s A_{s,prov} (d - x)]$							0.09		x10 <sup>-3</sup>
Mean strain, $\epsilon_m = \epsilon_1 - \epsilon_2$							1.47		x10 <sup>-3</sup>
Distance to face of extreme rebar, $c_f = \text{cover} + \text{MAX}(\phi_{link}, \phi_{link,t})$							35		mm
Distance to centroid of extreme rebar, $c = c_f + \phi_t / 2$							51		mm
Distance, $s = (b_w - 2 \cdot \text{cover} - 2 \cdot \text{MAX}(\phi_{link}, \phi_{link,t}) - \phi_t) / (n_t / n_{layers,tens} - 1)$							133		mm
Distance, $a_{c1} = [c^2 + c^2]^{1/2} - \phi_t / 2$							56		mm
Distance, $a_{c2} = [c^2 + (s/2)^2]^{1/2} - \phi_t / 2$							68		mm
Distance, $a_{cr} = \text{MAX}(a_{c1}, a_{c2})$							68		mm
<i>Note <math>a_{c1}</math> is not applicable for continuous width sections, i.e. slabs or walls;</i>									
									
Maximum crack width, $w_{max} = 3a_{cr} \epsilon_m / [1 + 2 \cdot (a_{cr} - c_f) / (h - x)]$							0.27		mm
Maximum crack width utilisation, $w_{max} / w_{allow} < 1.00$							89%		OK
<i>Note for a particular section and force / moment, crack widths can be reduced by increasing steel area, reducing spacing between rebars and reducing concrete cover (limited to durability requirements). The employment of smaller diameter bars at closer centres is thus preferable to larger diameter bars at further centres. There should be a provision for longitudinal steels at the side faces of beams of moderate depths;</i>									
Crack width utilisation							101%		NOT OK

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Job Title	Member Design - Reinforced Concrete Beam BS8110,				Drg. Ref.				
Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								EC2	
<b>Longitudinal Shear Between Web and Flange Rectangular or Flanged Beam (EC2)</b>									
<i>Note that this check is performed for both rectangular and flanged section designs, although theoretically only applicable in the latter case;</i>									
Longitudinal shear stress, $K_S \cdot v_{Ed}$					1.61	N/mm <sup>2</sup>			
Longitudinal shear stress, $v_{Ed} = \Delta F_d / (h_f \cdot \Delta x)$					1.21	N/mm <sup>2</sup>	cl.6.2.4		
Change of normal force in flange half over $\Delta x$ , $\Delta F_d = K_B \cdot (M^* - 0) / z$					606	kN			
<i>Note conservatively factor, <math>K_B = 0.5(b_{eff} - b_w) / b_{eff}</math> employed even if neutral axis within web;</i>									
Lever arm, $z$					0.763	m			
<i>Note if neutral axis within web, for simplicity, <math>z = d - h_f / 2</math>;</i>									
Thickness of the flange at the junctions, $h_f$					200	mm			
Length under consideration, $\Delta x$					2500	mm			
<i>Note the maximum value that may be assumed for <math>\Delta x</math> is half the distance between the section where the moment is 0 and the section where the moment is maximum. However, since <math>\Delta F_d</math> is also calculated over <math>\Delta x</math> based on a variation of moment of <math>\sim M/2 - 0</math> say, it is deemed acceptable to use for <math>\Delta x</math> the full distance between the section where the moment is 0 and the section where the moment is maximum based on a variation of moment of <math>M - 0</math> and factored by <math>K_S</math>.</i>								cl.6.2.4	
Shear stress distribution factor, $K_S$					1.33				
<i>For UDLs, <math>K_S</math> may be taken as 2.00 for simply supported beams, 1.33 for continuous beams and 2.00 for cantilever beams;</i>									
Effective width, $b_{eff} = \text{MIN}(b_w + \text{function (span, section, structure)})$					1000	mm			
<i>Note for rectangular sections, <math>b_{eff}</math> equivalent to that of T-sections assumed;</i>									
Width (rectangular) or web width (flanged), $b_w$					500	mm			
Longitudinal shear stress limit to prevent crushing, $v_{fcd} \sin \theta_f \cos \theta_f$					4.97	N/mm <sup>2</sup>	cl.6.2.4		
Design compressive strength, $f_{cd}$					19	N/mm <sup>2</sup>			
$f_{cd} = \alpha_{cc} f_{ck} / \gamma_c$ with $\alpha_{cc} = 1.0, \gamma_c = 1.5$					cl.3.1.6				
Strength reduction factor for concrete cracked in shear, $v$					0.533				
$v = 0.6 \left[ 1 - \frac{f_{ck}}{250} \right]$					cl.6.2.2				
Longitudinal shear stress limit to prevent crushing utilisation, $(K_S \cdot v_{Ed}) / (v_{fcd} \sin \theta_f \cos \theta_f)$					32%	OK			
Longitudinal shear stress limit for no transverse reinforcement, $0.4 f_{ctd}$					0.52	N/mm <sup>2</sup>	cl.6.2.4		
Design tensile strength, $f_{ctd}$					1.29	N/mm <sup>2</sup>			
$f_{ctd} = \alpha_{ct} f_{ctk,0.05} / \gamma_c$ with $\alpha_{ct} = 1.0, \gamma_c = 1.5$					cl.3.1.6				
$f_{ctk,0.05} = 0.7 \times f_{ctm}$					1.94	N/mm <sup>2</sup>	T.3.1		
$f_{ctm} = 0.30 \times f_{ck}^{(2/3)} \leq C50/60$ $f_{ctm} = 2.12 \cdot \ln(1 + (f_{cm}/10)) > C50/60$					2.77	N/mm <sup>2</sup>	T.3.1		
$f_{cm} = f_{ck} + 8 \text{ (MPa)}$					36	N/mm <sup>2</sup>	T.3.1		
Characteristic cylinder strength of concrete, $f_{ck}$					28	N/mm <sup>2</sup>	T.3.1		
Characteristic cube strength of concrete, $f_{cu}$					35	N/mm <sup>2</sup>	T.3.1		
Longitudinal shear stress limit for no transverse reinforcement utilisation, $(K_S \cdot v_{Ed}) / (v_{fcd} \sin \theta_f \cos \theta_f)$					312%	NOT OK			
Required design transverse reinforcement per unit length, $A_{sf}/s_f >$					741	mm <sup>2</sup> /m			
$(A_{sf} f_{yd} / s_f) \geq v_{Ed} \cdot h_f / \cot \theta_f$									
<i>Note area of transverse steel to be provided should be the greater of <math>1.0 A_{sf}/s_f</math> and <math>0.5 A_{sf}/s_f + \text{area required for slab bending}</math>; Note <math>K_S</math> factored onto <math>v_{Ed}</math> herein;</i>								cl.6.2.4	
Design yield strength of reinforcement, $f_{yd} = f_y / \gamma_s, \gamma_s = 1.15, f_y \leq 60$					435	N/mm <sup>2</sup>	.2.4, cl.3.2		
Thickness of the flange at the junctions, $h_f$					200	mm			
Angle, $\theta_f$					45.0	degrees			
$1.0 \leq \cot \theta_f \leq 2.0$ for compression flanges ( $45^\circ \geq \theta_f \geq 26.5^\circ$ ) $1.0 \leq \cot \theta_f \leq 1.25$ for tension flanges ( $45^\circ \geq \theta_f \geq 38.6^\circ$ )								cl.6.2.4	
Provided transverse reinforcement per unit length, $A_e$					785	mm <sup>2</sup> /m			
Required design transverse reinforcement per unit length utilisation, $(A_{sf}/s_f) /$					94%	OK			

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					jXXX	24																																											
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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.																																								
								BS5400-4																																									
<b>Longitudinal Shear Between Web and Flange Rectangular or Flanged Beam (BS5400-4)</b>																																																	
<i>Note that this check is performed for both rectangular and flanged section designs, although theoretically only applicable in the latter case;</i>																																																	
Longitudinal shear force per unit length, $V_1 = K_S \cdot \Delta F_d / \Delta x$					322	kN/m																																											
Change of normal force in flange half over $\Delta x$ , $\Delta F_d = K_B \cdot (M^* - 0) / z$					606	kN																																											
<i>Note conservatively factor, <math>K_B = 0.5(b_{eff} - b_w) / b_{eff}</math> employed even if neutral axis within web;</i>																																																	
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Length under consideration, $\Delta x$					2500	mm																																											
<i>Note <math>\Delta x</math> is the beam length between the point of maximum design moment and the point of zero moment;</i>																																																	
Shear stress distribution factor, $K_S$					1.33																																												
<i>The longitudinal shear should be calculated per unit length. For UDLs, <math>K_S</math> may be taken as 2.00 for simply supported beams, 1.33 for continuous beams and 2.00 for cantilever beams;</i>								cl.7.4.2.3																																									
Effective width, $b_{eff} = \text{MIN}(b_w + \text{function (span, section, structure)})$					1000	mm																																											
<i>Note for rectangular sections, <math>b_{eff}</math> equivalent to that of T-sections assumed;</i>																																																	
Width (rectangular) or web width (flanged), $b_w$					500	mm																																											
Longitudinal shear force limit per unit length, $V_{1,limit}$					503	kN/m																																											
<div style="border: 1px solid black; padding: 5px;"> <math>V_1</math> should not exceed the lesser of the following:            a) <math>k_1 f_{cu} L_s</math>            b) <math>v_1 L_s + 0.7 A_e f_y</math> </div>					(a)	1050	kN/m	cl.7.4.2.3																																									
					(b)	503	kN/m	cl.7.4.2.3																																									
<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th colspan="6" style="text-align: center;">Table 31 — Ultimate longitudinal shear stress, <math>v_1</math>, and values of <math>k_1</math> for composite members</th> </tr> <tr> <th rowspan="2" style="text-align: center;">Type of shear plane</th> <th colspan="4" style="text-align: center;">Longitudinal shear stress for concrete grade</th> <th rowspan="2" style="text-align: center;"><math>k_1</math></th> </tr> <tr> <th style="text-align: center;">20</th> <th style="text-align: center;">25</th> <th style="text-align: center;">30</th> <th style="text-align: center;">40 or more</th> </tr> <tr> <td></td> <th style="text-align: center;">N/mm<sup>2</sup></th> <th style="text-align: center;">N/mm<sup>2</sup></th> <th style="text-align: center;">N/mm<sup>2</sup></th> <th style="text-align: center;">N/mm<sup>2</sup></th> <td></td> </tr> </thead> <tbody> <tr> <td>Monolithic construction</td> <td style="text-align: center;">0.90</td> <td style="text-align: center;">0.90</td> <td style="text-align: center;">1.25</td> <td style="text-align: center;">1.25</td> <td style="text-align: center;">0.15</td> </tr> <tr> <td>Surface type 1</td> <td style="text-align: center;">0.50</td> <td style="text-align: center;">0.63</td> <td style="text-align: center;">0.75</td> <td style="text-align: center;">0.80</td> <td style="text-align: center;">0.15</td> </tr> <tr> <td>Surface type 2</td> <td style="text-align: center;">0.30</td> <td style="text-align: center;">0.38</td> <td style="text-align: center;">0.45</td> <td style="text-align: center;">0.50</td> <td style="text-align: center;">0.09</td> </tr> </tbody> </table> <p style="font-size: small;">NOTE For construction with lightweight aggregate concrete, the values given in this table should be reduced by 25 %.</p>										Table 31 — Ultimate longitudinal shear stress, $v_1$ , and values of $k_1$ for composite members						Type of shear plane	Longitudinal shear stress for concrete grade				$k_1$	20	25	30	40 or more		N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>		Monolithic construction	0.90	0.90	1.25	1.25	0.15	Surface type 1	0.50	0.63	0.75	0.80	0.15	Surface type 2	0.30	0.38	0.45	0.50	0.09
Table 31 — Ultimate longitudinal shear stress, $v_1$ , and values of $k_1$ for composite members																																																	
Type of shear plane	Longitudinal shear stress for concrete grade				$k_1$																																												
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Monolithic construction	0.90	0.90	1.25	1.25	0.15																																												
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Surface type 2	0.30	0.38	0.45	0.50	0.09																																												
Concrete bond constant, $k_1$					0.15			T.31																																									
Ultimate longitudinal shear stress limit, $v_1$					1.25	N/mm <sup>2</sup>	T.31																																										
Surface type					Monolithic construction	▼	T.31																																										
Length of shear plane, $L_s = h_f$					200	mm																																											
Provided transverse reinforcement per unit length, $A_e$					785	mm <sup>2</sup> /m																																											
<i>Note reinforcement provided for coexistent bending effects and shear reinforcement crossing the shear plane, provided to resist vertical shear, may be included provided they are fully anchored;</i>								cl.7.4.2.3																																									
Characteristic strength of reinforcement, $f_y \leq 460 \text{ N/mm}^2$					460	N/mm <sup>2</sup>																																											
Longitudinal shear force limit per unit length utilisation, $V_1 / V_{1,limit}$					64%			OK																																									
Required nominal transverse reinforcement per unit length, $0.15\% L_s$					300	mm <sup>2</sup> /m	cl.7.4.2.3																																										
Required nominal transverse reinforcement per unit length utilisation, $0.15\%$					38%			OK																																									



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					jXXX	25			
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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								EC2	
<b>Longitudinal Shear Within Web Rectangular or Flanged Beam (EC2)</b>									
Longitudinal shear stress, $V_{Edi} = \beta V_{Ed} / (z b_i)$					1.53	N/mm <sup>2</sup>	cl.6.2.5		
Ratio, $\beta = 1.0$					1.0		cl.6.2.5		
Transverse shear force (averaged), $V_{Ed} = V_d^*/2$					585	kN	cl.6.2.5		
Lever arm, z					0.763	m	cl.6.2.5		
<i>Note if neutral axis within web, for simplicity, <math>z = d - h_f/2</math>;</i>									
Width of the interface, $b_i = b_w$					500	mm	cl.6.2.5		
Longitudinal shear stress limit, $V_{Rdi}$					3.10	N/mm <sup>2</sup>			
$V_{Rdi} = c f_{ctd} + \mu \sigma_n + \rho f_{yd} (\mu \sin \alpha + \cos \alpha) \leq 0,5 v f_{cd}$							cl.6.2.5		
<i>Note <math>c.f_{ctd} = 0.00</math> if <math>\sigma_n</math> is negative (tension);</i>									
Roughness coefficient, c					Indented	▼	0.500	cl.6.2.5	
Roughness coefficient, $\mu$					Indented	▼	0.9	cl.6.2.5	
<p>Very smooth: a surface cast against steel, plastic or specially prepared wooden moulds: <math>c = 0,025</math> to <math>0,10</math> and <math>\mu = 0,5</math></p> <p>Smooth: a slipformed or extruded surface, or a free surface left without further treatment after vibration: <math>c = 0,20</math> and <math>\mu = 0,6</math></p> <p>Rough: a surface with at least 3 mm roughness at about 40 mm spacing, achieved by raking, exposing of aggregate or other methods giving an equivalent behaviour: <math>c = 0,40</math> and <math>\mu = 0,7</math> <small>(ACI)</small></p> <p>Indented: a surface with indentations complying with Figure 6.9: <math>c = 0,50</math> and <math>\mu = 0,9</math></p>									
Design tensile strength, $f_{ctd}$					1.29	N/mm <sup>2</sup>			
$f_{ctd} = \alpha_{ct} f_{ctk,0.05} / \gamma_c$ with $\alpha_{ct} = 1.0, \gamma_c = 1.5$							cl.3.1.6		
$f_{ctk,0.05} = 0,7 \times f_{ctm}$					1.94	N/mm <sup>2</sup>	T.3.1		
$f_{ctm} = 0,30 \times f_{ck}^{(2/3)} \leq C50/60$ $f_{ctm} = 2,12 \cdot \ln(1 + (f_{cm}/10)) > C50/60$					2.77	N/mm <sup>2</sup>	T.3.1		
$f_{cm} = f_{ck} + 8$ (MPa)					36	N/mm <sup>2</sup>	T.3.1		
Characteristic cylinder strength of concrete, $f_{ck}$					28	N/mm <sup>2</sup>	T.3.1		
Characteristic cube strength of concrete, $f_{cu}$					35	N/mm <sup>2</sup>	T.3.1		
Normal stress across longitudinal shear interface, $\sigma_n = 0$					0.00	N/mm <sup>2</sup>			
Reinforcement ratio, $\rho = A_s / A_i$					0.006		cl.6.2.5		
Area of reinforcement, $A_s = A_{sv,prov}/S + A_{sv,prov,t}/S_t$					3142	mm <sup>2</sup> /m			
<i>Note that the area of reinforcement crossing the shear interface may include ordinary shear reinforcement with adequate anchorage at both sides of the interface;</i>									
Area of the joint, $A_i = 1000 \cdot b_i$					500000	mm <sup>2</sup> /m			
Design yield strength of reinforcement, $f_{yd} = f_{yv}/\gamma_s, \gamma_s = 1.15, f_{yv} \leq 6$					435	N/mm <sup>2</sup>	.2.4, cl.3.2		
Angle of reinforcement, $\alpha = 90.0^\circ$					90.0	degrees	cl.6.2.5		
Design compressive strength, $f_{cd}$					19	N/mm <sup>2</sup>			
$f_{cd} = \alpha_{cc} f_{ck} / \gamma_c$ with $\alpha_{cc} = 1.0, \gamma_c = 1.5$							cl.3.1.6		
Strength reduction factor for concrete cracked in shear, v					0.533				
$v = 0,6 \left[ 1 - \frac{f_{ck}}{250} \right]$							cl.6.2.2		
Longitudinal shear stress limit utilisation, $V_{Edi}/V_{Rdi}$					49%		OK		

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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.																																		
								BS8110																																			
<b>Longitudinal Shear Within Web Rectangular or Flanged Beam (BS8110)</b>																																											
Longitudinal shear stress, $v_h = K_S \cdot \Delta F_c / (b_w \Delta x)$					2.58	N/mm <sup>2</sup>	cl.5.4.7.2																																				
Change of total compression force over $\Delta x$ , $\Delta F_c = (M-0)/z$					2423	kN	cl.5.4.7.1																																				
Lever arm, $z$					0.763	m																																					
<i>Note if neutral axis within web, for simplicity, <math>z = d - h_f/2</math>;</i>																																											
Length under consideration, $\Delta x$					2500	mm																																					
<i>Note <math>\Delta x</math> is the beam length between the point of maximum design moment and the point of zero moment;</i>					cl.5.4.7.2																																						
Shear stress distribution factor, $K_S$					1.33																																						
<i>The average design shear stress should then be distributed in proportion to the vertical design shear force diagram to give the horizontal shear stress at any point along the length of the member. For UDLs, <math>K_S</math> maybe taken as 2.00 for simply supported beams, 1.33 for continuous beams and 2.00 for cantilever beams;</i>					cl.5.4.7.2																																						
Width (rectangular) or web width (flanged), $b_w$					500	mm																																					
Longitudinal shear stress limit for no nominal / design vertical reinforcement					2.35	N/mm <sup>2</sup>																																					
Surface type					Washed to remove laitance etc		T.5.5																																				
<table border="1" style="width: 100%; border-collapse: collapse;"> <caption>Table 5.5 — Design ultimate horizontal shear stresses at interface</caption> <thead> <tr> <th rowspan="2">Precast unit</th> <th rowspan="2">Surface type</th> <th colspan="3">Grade of in-situ concrete</th> </tr> <tr> <th>25 N/mm<sup>2</sup></th> <th>30 N/mm<sup>2</sup></th> <th>40 and over N/mm<sup>2</sup></th> </tr> </thead> <tbody> <tr> <td rowspan="3">Without links</td> <td>As-cast or as-extruded</td> <td>0.4</td> <td>0.55</td> <td>0.65</td> </tr> <tr> <td>Brushed, screeded or rough-tamped</td> <td>0.6</td> <td>0.65</td> <td>0.75</td> </tr> <tr> <td>Washed to remove laitance or treated with retarder and cleaned</td> <td>0.7</td> <td>0.75</td> <td>0.80</td> </tr> <tr> <td rowspan="3">With nominal links projecting into in-situ concrete</td> <td>As-cast or as-extruded</td> <td>1.2</td> <td>1.8</td> <td>2.0</td> </tr> <tr> <td>Brushed, screeded or rough-tamped</td> <td>1.8</td> <td>2.0</td> <td>2.2</td> </tr> <tr> <td>Washed to remove laitance or treated with retarder and cleaned</td> <td>2.1</td> <td>2.2</td> <td>2.5</td> </tr> </tbody> </table> <p>NOTE 1 The description "as-cast" covers those cases where the concrete is placed and vibrated leaving a rough finish. The surface is rougher than would be required for finishes to be applied directly without a further finishing screed but not as rough as would be obtained if tamping, brushing or other artificial roughening had taken place.</p> <p>NOTE 2 The description "as-extruded" covers those cases in which an open-textured surface is produced direct from an extruding machine.</p> <p>NOTE 3 The description "brushed, screeded or rough-tamped" covers those cases where some form of deliberate surface roughening has taken place but not to the extent of exposing the aggregate.</p> <p>NOTE 4 For structural assessment purposes, it may be assumed that the appropriate value of <math>\gamma_m</math> included in the table is 1.5.</p>										Precast unit	Surface type	Grade of in-situ concrete			25 N/mm <sup>2</sup>	30 N/mm <sup>2</sup>	40 and over N/mm <sup>2</sup>	Without links	As-cast or as-extruded	0.4	0.55	0.65	Brushed, screeded or rough-tamped	0.6	0.65	0.75	Washed to remove laitance or treated with retarder and cleaned	0.7	0.75	0.80	With nominal links projecting into in-situ concrete	As-cast or as-extruded	1.2	1.8	2.0	Brushed, screeded or rough-tamped	1.8	2.0	2.2	Washed to remove laitance or treated with retarder and cleaned	2.1	2.2	2.5
Precast unit	Surface type	Grade of in-situ concrete																																									
		25 N/mm <sup>2</sup>	30 N/mm <sup>2</sup>	40 and over N/mm <sup>2</sup>																																							
Without links	As-cast or as-extruded	0.4	0.55	0.65																																							
	Brushed, screeded or rough-tamped	0.6	0.65	0.75																																							
	Washed to remove laitance or treated with retarder and cleaned	0.7	0.75	0.80																																							
With nominal links projecting into in-situ concrete	As-cast or as-extruded	1.2	1.8	2.0																																							
	Brushed, screeded or rough-tamped	1.8	2.0	2.2																																							
	Washed to remove laitance or treated with retarder and cleaned	2.1	2.2	2.5																																							
Longitudinal shear stress limit for no nominal / design vertical reinforcement					110%		NOT OK																																				
.2(3)																																											
Required nominal vertical reinforcement per unit length, $0.15\%b_w$					750	mm <sup>2</sup> /m	cl.5.4.7.3																																				
Provided vertical reinforcement per unit length, $A_e$					3142	mm <sup>2</sup> /m																																					
<i>Note <math>A_e = A_{sv,prov} / S + A_{sv,prov,t} / S_t</math>;</i>																																											
Required nominal vertical reinforcement per unit length utilisation, $0.15\%b_w$					24%		OK																																				
<i>Note UT set to 0% if longitudinal shear stress limit for no nominal vertical reinforcement <math>UT \leq 100\%</math>;</i>																																											
Required design vertical reinforcement per unit length, $A_h$					2949	mm <sup>2</sup> /m																																					
$A_h = \frac{1000bv_h}{0.95f_y}$																																											
<i>Note <math>f_{yv} \leq 460\text{N/mm}^2</math></i>					cl.5.4.7.4, Fore																																						
Required design vertical reinforcement per unit length utilisation, $A_h/A_e$					94%		OK																																				
<i>Note UT set to 0% if longitudinal shear stress limit for no design vertical reinforcement <math>UT \leq 100\%</math>;</i>																																											

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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.																																		
								BS5400-4																																			
<b>Longitudinal Shear Within Web Rectangular or Flanged Beam (BS5400-4)</b>																																											
Longitudinal shear force per unit length, $V_1 = K_S \cdot \Delta F_c / \Delta x$					1289	kN/m																																					
Change of total compression force over $\Delta x$ , $\Delta F_c = (M-0)/z$					2423	kN																																					
Lever arm, $z$					0.763	m																																					
<i>Note if neutral axis within web, for simplicity, <math>z = d - h_f/2</math>;</i>																																											
Length under consideration, $\Delta x$					2500	mm																																					
<i>Note <math>\Delta x</math> is the beam length between the point of maximum design moment and the point of zero moment;</i>																																											
Shear stress distribution factor, $K_S$					1.33																																						
<i>The longitudinal shear should be calculated per unit length. For UDLs, <math>K_S</math> may be taken as 2.00 for simply supported beams, 1.33 for continuous beams and 2.00 for cantilever beams;</i>								cl.7.4.2.3																																			
Width (rectangular) or web width (flanged), $b_w$					500	mm																																					
Longitudinal shear force limit per unit length, $V_{1,limit}$					1637	kN/m																																					
<div style="border: 1px solid black; padding: 5px;"> <math>V_1</math> should not exceed the lesser of the following:            a) <math>k_1 f_{cu} L_s</math>            b) <math>v_1 L_s + 0.7 A_e f_y</math> </div>					(a)	2625	kN/m	cl.7.4.2.3																																			
					(b)	1637	kN/m	cl.7.4.2.3																																			
<table border="1" style="width: 100%; border-collapse: collapse;"> <caption>Table 31 — Ultimate longitudinal shear stress, <math>v_1</math>, and values of <math>k_1</math> for composite members</caption> <thead> <tr> <th rowspan="2">Type of shear plane</th> <th colspan="4">Longitudinal shear stress for concrete grade</th> <th rowspan="2"><math>k_1</math></th> </tr> <tr> <th>20</th> <th>25</th> <th>30</th> <th>40 or more</th> </tr> <tr> <td></td> <td>N/mm<sup>2</sup></td> <td>N/mm<sup>2</sup></td> <td>N/mm<sup>2</sup></td> <td>N/mm<sup>2</sup></td> <td></td> </tr> </thead> <tbody> <tr> <td>Monolithic construction</td> <td>0.90</td> <td>0.90</td> <td>1.25</td> <td>1.25</td> <td>0.15</td> </tr> <tr> <td>Surface type 1</td> <td>0.50</td> <td>0.63</td> <td>0.75</td> <td>0.80</td> <td>0.15</td> </tr> <tr> <td>Surface type 2</td> <td>0.30</td> <td>0.38</td> <td>0.45</td> <td>0.50</td> <td>0.09</td> </tr> </tbody> </table> <p>NOTE For construction with lightweight aggregate concrete, the values given in this table should be reduced by 25 %.</p>										Type of shear plane	Longitudinal shear stress for concrete grade				$k_1$	20	25	30	40 or more		N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>		Monolithic construction	0.90	0.90	1.25	1.25	0.15	Surface type 1	0.50	0.63	0.75	0.80	0.15	Surface type 2	0.30	0.38	0.45	0.50	0.09
Type of shear plane	Longitudinal shear stress for concrete grade				$k_1$																																						
	20	25	30	40 or more																																							
	N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>	N/mm <sup>2</sup>																																							
Monolithic construction	0.90	0.90	1.25	1.25	0.15																																						
Surface type 1	0.50	0.63	0.75	0.80	0.15																																						
Surface type 2	0.30	0.38	0.45	0.50	0.09																																						
Concrete bond constant, $k_1$					0.15			T.31																																			
Ultimate longitudinal shear stress limit, $v_1$					1.25	N/mm <sup>2</sup>	T.31																																				
Surface type					Monolithic construction	▼	T.31																																				
Length of shear plane, $L_s = b_w$					500	mm																																					
Provided vertical reinforcement per unit length, $A_e$					3142	mm <sup>2</sup> /m																																					
<i>Note <math>A_e = A_{sv,prov} / S + A_{sv,prov,t} / S_t</math>;</i>																																											
<i>Note reinforcement provided for coexistent bending effects and shear reinforcement crossing the shear plane, provided to resist vertical shear, may be included provided they are fully anchored;</i>								cl.7.4.2.3																																			
Characteristic strength of reinforcement, $f_{yv} \leq 460$ N/mm <sup>2</sup>					460	N/mm <sup>2</sup>																																					
Longitudinal shear force limit per unit length utilisation, $V_1/V_{1,limit}$					79%			OK																																			
Required nominal vertical reinforcement per unit length, $0.15\%L_s$					750	mm <sup>2</sup> /m	cl.7.4.2.3																																				
Required nominal vertical reinforcement per unit length utilisation, $0.15\%L_s/$					24%			OK																																			
<i>Note UT set to 0% if longitudinal shear force limit per unit length for no nominal vertical reinforcement</i>																																											
<i>UT &lt;= 100%;</i>																																											



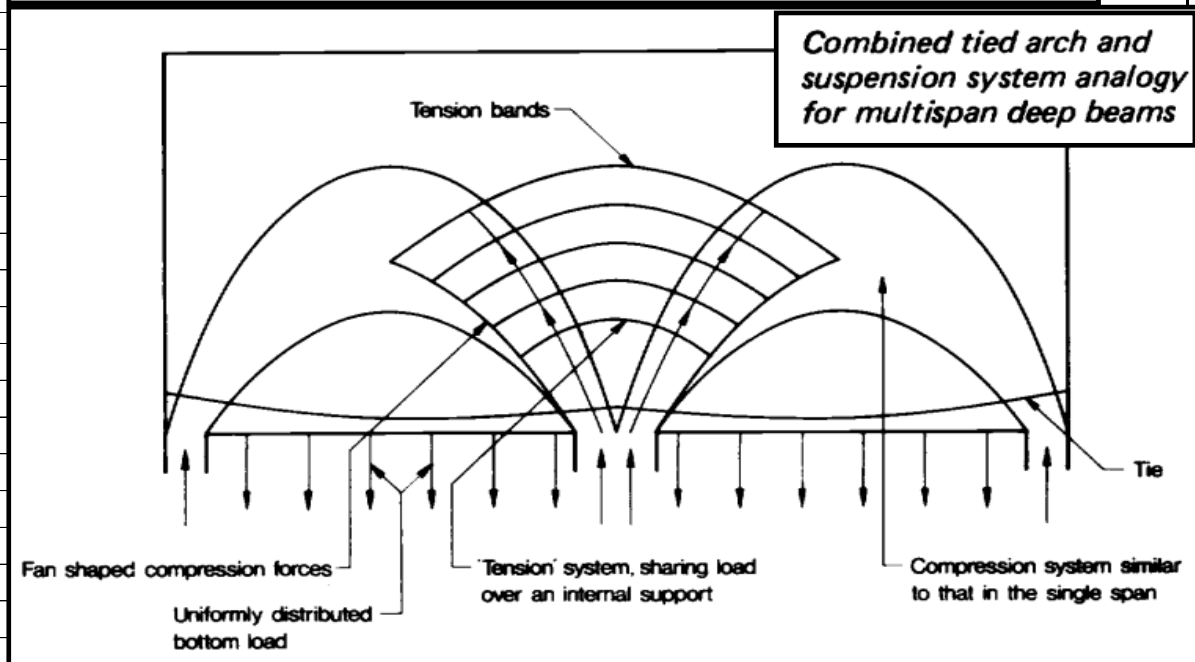
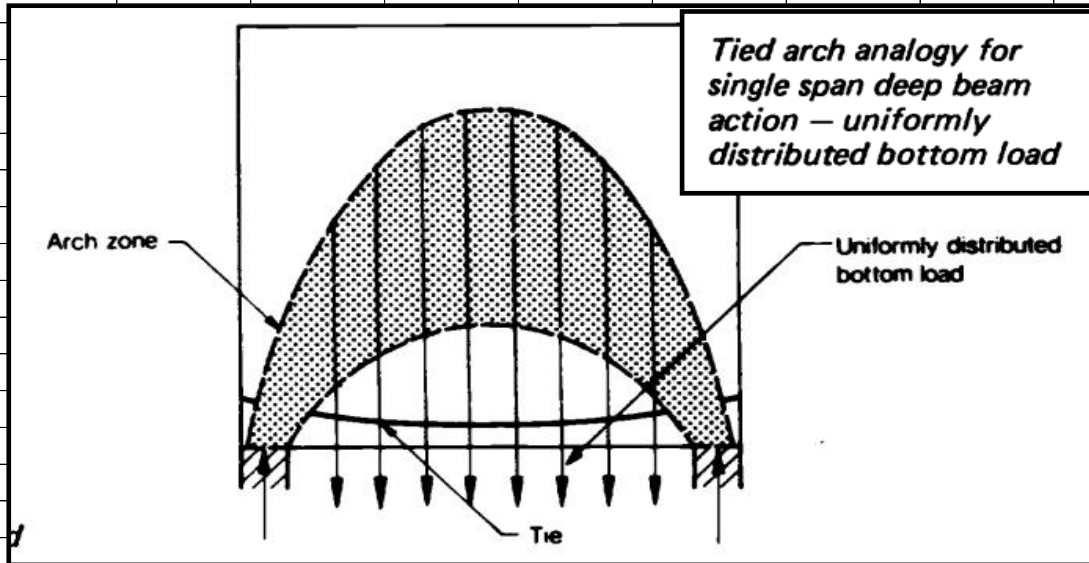
CONSULTING ENGINEERS		Engineering Calculation Sheet Consulting Engineers			Job No.	Sheet No.	Rev.		
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Job Title	Member Design - Reinforced Concrete Beam BS8110,				Drg. Ref.				
Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								BS8110	
<b>Deep Beam Bending</b>								Reynolds	
Design bending moment, M								N/A kNm	
Tension steel (deep beam), $A_{s,db} = 1.75M / [f_y \cdot h]$ , $f_y \leq 460\text{N/mm}^2$								N/A mm <sup>2</sup>	T.148
<i>Note that the factor 1.75 is obtained from 1 / (lever arm factor 0.6 x material factor 0.95);</i>								cl.21.4.1	
Tension steel zone depth, $T_{zone}$ (sag s/s, sag cont, hog cant)								N/A mm	cl.21.4.1
Tension steel zone depth, $T_{zone}$ (hog cont)								N/A mm	
<i>Note <math>A_{s,db}</math> to be distributed over depth of <math>T_{zone}</math> from tension face;</i>								cl.21.4.1	
<i>Note <math>T_{zone} = (5h - span_{lim}) / 20</math> s/s sag and cont sag, <math>(5h - 2 \times span_{lim}) / 20</math> cant hog;</i>								cl.21.4.1 / SE	
Tension steel area provided (deep beam)								N/A mm <sup>2</sup>	
Tension steel area provided (deep beam) utilisation								N/A	N/A
<b>Deep Beam Shear</b>								Reynolds	
Design shear force, $V_d$								N/A kN	
<i>Note the ultimate shear force limit is <math>b_w \cdot h \cdot f_c' / 10 \gamma_m</math> where <math>f_c'</math> is the cylinder comp strength and</i>								cl.21.4.1	
Ultimate shear force utilisation								N/A	N/A
Area of tension steel reinforcement provided, $A_{s,prov}$								N/A mm <sup>2</sup>	
Clear distance from edge of load to face of support, $a_1$								DL @ mid 0.625h	T.148
<i>Note for UDLs, concentrate total UDL at {span/4 s/s and cont, span/2 cant} from the support(s);</i>								T.148	
Ratio $a_1/h$								N/A	N/A
<i>Note ensure <math>a_1/h</math> is not greatly outside range of 0.23 to 0.70;</i>								T.148	
Angle between horizontal bar and critical diagonal crack, $\theta = \tan^{-1} (h/a_1)$								N/A degrees	T.148
Empirical coefficient, $k_1 = \{0.70 \text{ NWC}, 0.50 \text{ LWC}\}$								N/A	T.148
Empirical coefficient, $k_2 = \{100 \text{ plain round bars}, 225 \text{ deformed bars}\}$								N/A N/mm <sup>2</sup>	T.148
Cylinder splitting tensile strength, $f_t = 0.5(f_{cu})^{0.5}$								N/A N/mm <sup>2</sup>	T.148
Minimum breadth for deep beam, $b_w \approx \text{MAX} \{0, 0.65V_d/[k_1 \cdot (h-0.35a_1) \cdot f_t]\}$								N/A mm	N/A
Number of rows of horizontal shear links in a vertical cross-section, n								N/A	
<i>Note the no. of rows of horizontal shear links reduced to account for <math>T_{zone}</math>, i.e. <math>(h - T_{zone})/S_h</math>;</i>									
Design horizontal links shear capacity, $V_r = k_2 \Sigma A_{sv,prov,h} \cdot a_2 \cdot \sin^2 \theta / h$								N/A kN	T.148
<i>Note the summation of the depths at which the horizontal shear links intersect the diagonal crack, <math>\Sigma a_2</math> is calculated as <math>S_h \cdot n \cdot (n+1)/2</math> where n is the number of rows of horizontal shear links;</i>									
<b>Check <math>V_d &lt; 1.0V_1</math> for no horizontal links (minor elements)</b>								N/A	T.148
Concrete shear capacity, $V_1$								N/A kN	T.148
<i>Note <math>V_1 = \text{MAX}[0, k_1 \cdot (h-0.35a_1) \cdot f_t \cdot b_w] + k_2 \cdot A_{s,prov} \cdot d \cdot \sin^2 \theta / h</math>;</i>								T.148	
<b>Check <math>V_d &gt; 0.0</math> for design horizontal links</b>								N/A	T.148
Concrete and design horizontal links shear capacity $V_r + V_1$								N/A kN	T.148
Design shear resistance (deep beam) utilisation								N/A	N/A

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Member Design - RC Beam					Made by	XX	Date	16/1/2024	Chd.
								BS8110	
<b>Deep Beam Bending</b>								CIRIA	
								Guide 2	
Design bending moment, M					N/A	kNm			
Note the ultimate bending moment limit is $0.12f_{cu}b_w h^2$ ;								cl.2.4.1	
Ultimate bending moment utilisation					N/A			N/A	
Tension steel (deep beam), $A_{s,db} = M / [0.95f_y z]$ , $f_y \leq 460 \text{N/mm}^2$					N/A	mm <sup>2</sup>		cl.2.4.1	
Lever arm at which the tension steel (deep beam) acts, z					N/A		mm		cl.2.4.1
Simply supported, $z = 0.2 \times \text{span}_{lim} + 0.4h$					N/A		mm		cl.2.4.1
LF	Continuous, $z = 0.2 \times \text{span}_{lim} + 0.3h$				N/A		mm		cl.2.4.1
Cantilever, $z = 0.4 \times \text{span}_{lim} + 0.4h$					N/A		mm		SELF
Tension steel zone depth, $T_{zone}$ (sag s/s, sag cont, hog cant)					N/A		mm		cl.2.4.1
Tension steel zone depth, $T_{zone}$ (hog cont) upper band					N/A	N/A		mm	cl.2.4.1
Tension steel zone depth, $T_{zone}$ (hog cont) lower band					N/A	N/A		mm	cl.2.4.1
Note $A_{s,db}$ to be distributed over depth of $T_{zone}$ from tension face;								cl.2.4.1	
Note $T_{zone} = 0.2h$ s/s sag, cont sag and cant hog;								cl.2.4.1	
Note $T_{zone} = 0.2h$ cont hog upper band $0.5(\text{span}_{lim}/h-1)A_{s,db}$ , $0.2h-0.8h$ cont hog lower band remainder;									
Tension steel area provided (deep beam)					N/A		mm <sup>2</sup>		
Tension steel area provided (deep beam) utilisation					N/A				N/A
<b>Deep Beam Shear</b>								CIRIA	
								Guide 2	
Design shear force, $V_d$					N/A		kN		
Note the ultimate shear force limit is $\min\{b_w \cdot h \cdot v_u, 2b_w \cdot h^2 \cdot v_c k_s / x_e\}$ where $v_u$ is the ultimate concrete shear strength from CP 110 T.6 and T.26 replaced by $\min\{0.8f_{cu}^{0.5}, \{5.0, 7.0\} \text{N/mm}^2\}$ and $v_c$ is the design concrete shear strength from CP 110 T.5 and T.25 replaced by $v_c$ ;								cl.2.4.2	
Factor, $k_s = 1.0$ for $h/b_w < 4$ , else $0.6$					N/A				cl.2.4.2
Ultimate shear force utilisation					N/A				N/A
Area of tension steel reinforcement provided, $A_{s,prov}$					N/A		mm <sup>2</sup>		
Clear distance from edge of load to face of support, $x_e$					DL @ mid $0.625h$	N/A		mm	cl.2.4.2
Note for UDLs, concentrate total UDL at $\{\text{span}/4$ s/s and cont, $\text{span}/2$ cant $\}$ from the support(s);								cl.2.4.2	
Ratio $x_e/h$					N/A				N/A
Note ensure $x_e/h$ is not greatly outside range of $0.23$ to $0.70$ ;								cl.3.4.2	
Angle between horizontal bar and critical diagonal crack, $\theta = \tan^{-1}(h/x_e)$					N/A		degrees		cl.2.4.2
Empirical coefficient, $\lambda_1 = \{0.44 \text{ NWC}, 0.32 \text{ LWC}\}$					N/A				cl.3.4.2
Empirical coefficient, $\lambda_2 = \{0.85 \text{ plain round bars}, 1.95 \text{ deformed bars}\}$					N/A		N/mm <sup>2</sup>		cl.3.4.2
Number of rows of horizontal shear links in a vertical cross-section, n					N/A				
Note the no. of rows of horizontal shear links reduced to account for $T_{zone}$ , i.e. $(h - T_{zone})/S_h$ ;									
Design horizontal links shear capacity, $V_r = 100\lambda_2 \Sigma A_{sv,prov,h} \cdot \gamma_r \cdot \sin^2 \theta / h$					N/A		kN		cl.3.4.2
Note the summation of the depths at which the horizontal shear links intersect the diagonal crack, $\Sigma \gamma_r$ is calculated as $S_h \cdot n \cdot (n+1)/2$ where n is the number of rows of horizontal shear links;									
<b>Check <math>V_d &lt; 1.0V</math> for no horizontal links (minor elements)</b>					N/A				cl.3.4.2
Concrete shear capacity, $V (\leq 1.3\lambda_1 \sqrt{f_{cu}} \cdot b_w \cdot h)$					N/A		kN		cl.3.4.2
Note $V = \text{MAX}[0, \lambda_1 \cdot (h - 0.35x_e) \cdot \sqrt{f_{cu}} \cdot b_w] + 100 \lambda_2 \cdot A_{s,prov} \cdot d \cdot \sin^2 \theta / h$ ;								cl.3.4.2	
Note require $[100 \lambda_2 \cdot A_{s,prov} \cdot d \cdot \sin^2 \theta / h] / V \geq 0.20$ ;								N/A	N/A
<b>Check <math>V_d &gt; 0.0</math> for design horizontal links</b>					N/A				cl.3.4.2
Concrete and design horizontal links shear capacity $V_r + V (\leq \lambda_1 \cdot v_{max} \cdot b_w \cdot h)$					N/A		kN		cl.3.4.2
Note $v_{max} = 1.3 \sqrt{f_{cu}}$ ;								T.5	
Note require $[V_r + 100 \lambda_2 \cdot A_{s,prov} \cdot d \cdot \sin^2 \theta / h] / [V_r + V] \geq 0.20$ ;								N/A	N/A
Design shear resistance (deep beam) utilisation					N/A				N/A

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BS8110

**Detailing Instructions (Deep Beam)**



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Member Design - RC Beam		XX	16/1/2024	
				BS8110

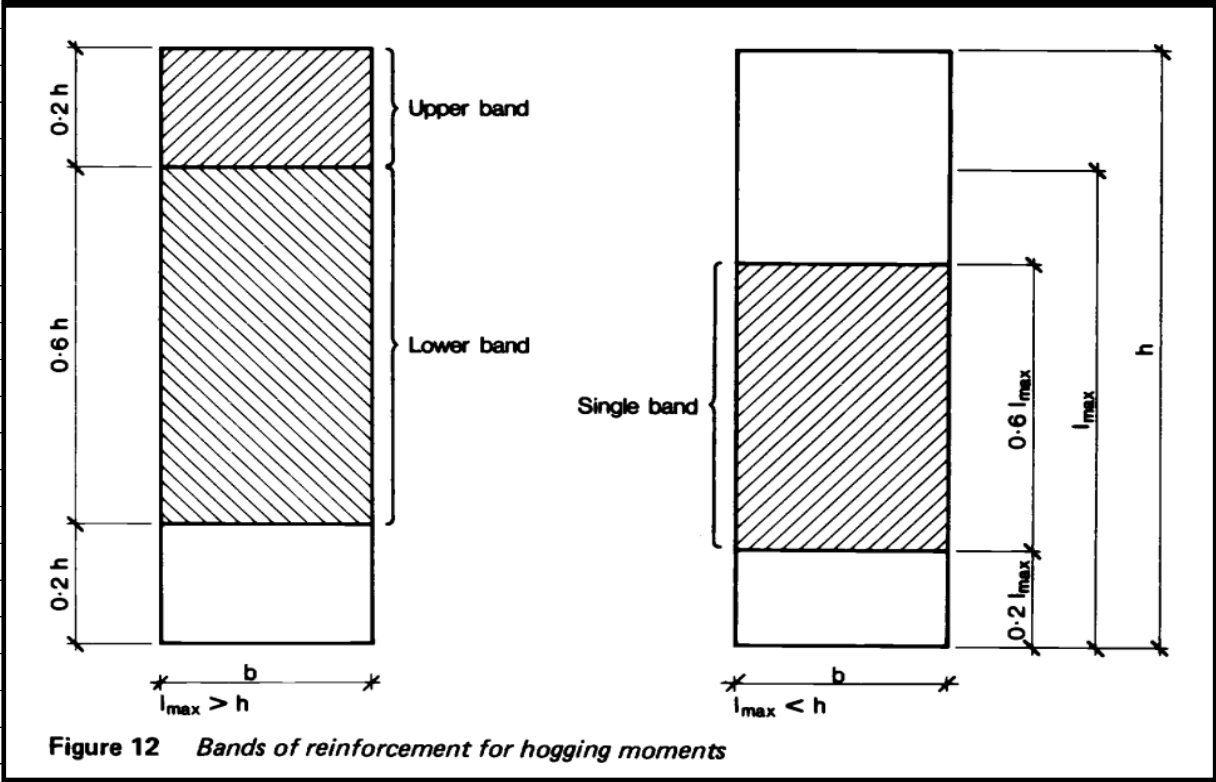
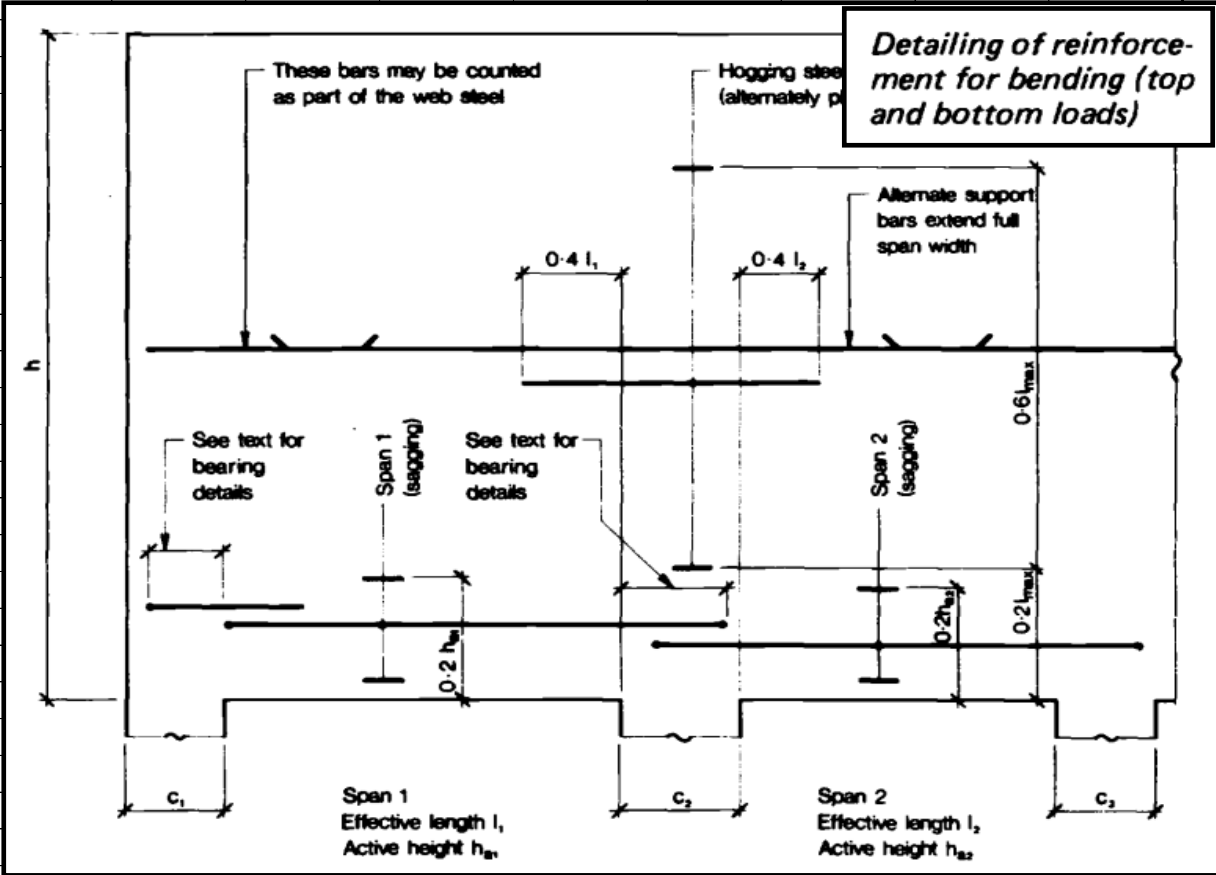
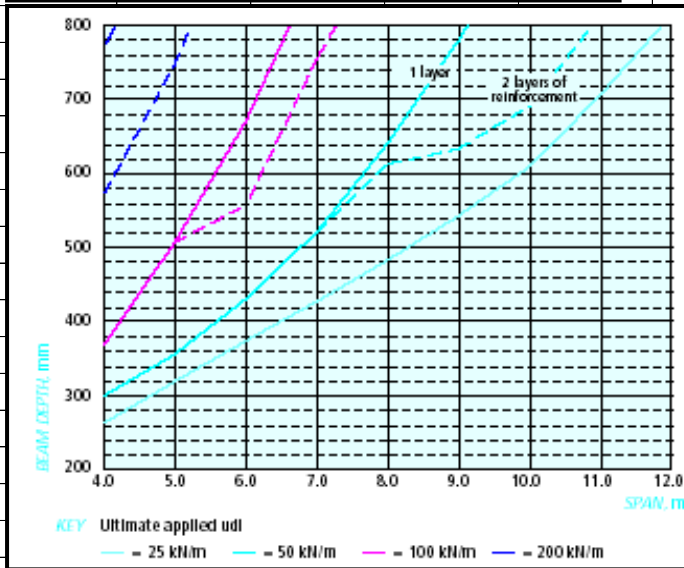
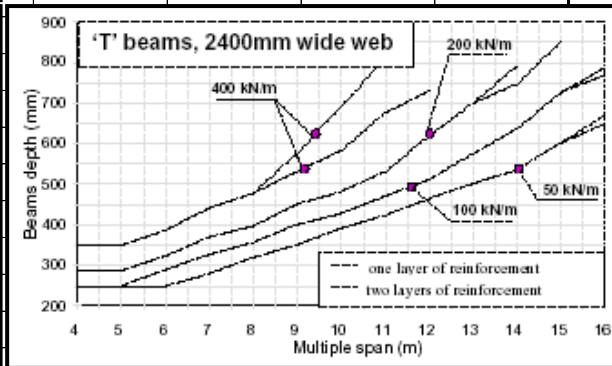
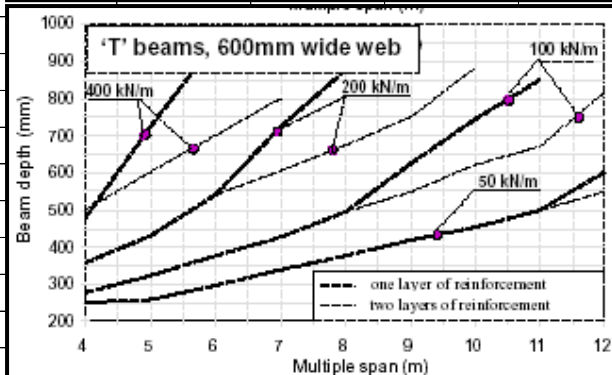
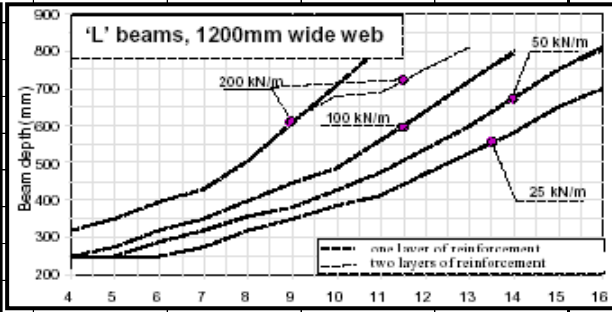
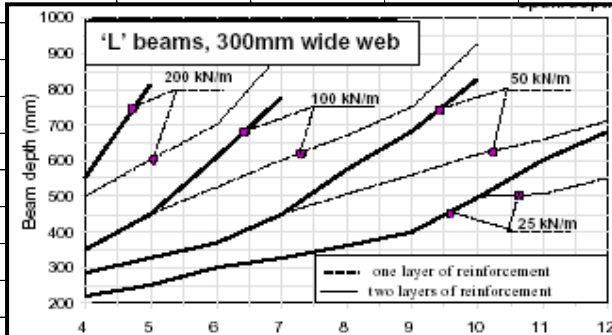


Figure 12 Bands of reinforcement for hogging moments



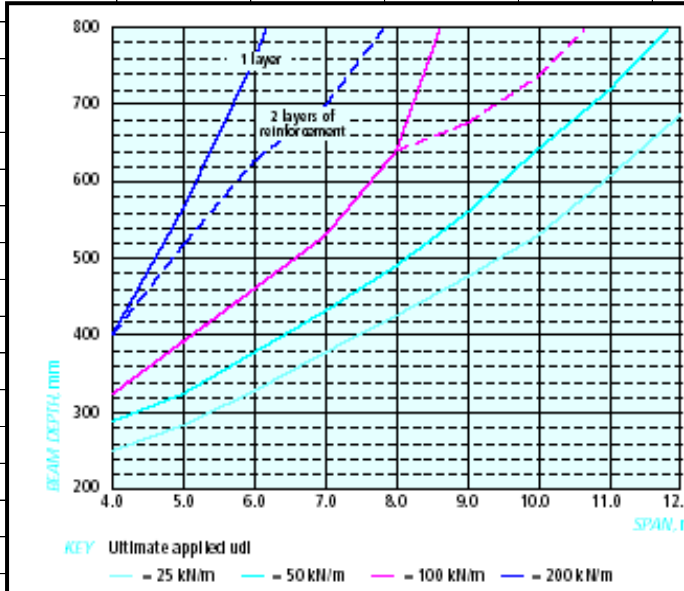
**Scheme Design**



Rectangular beams

**300 mm**  
wide

single span

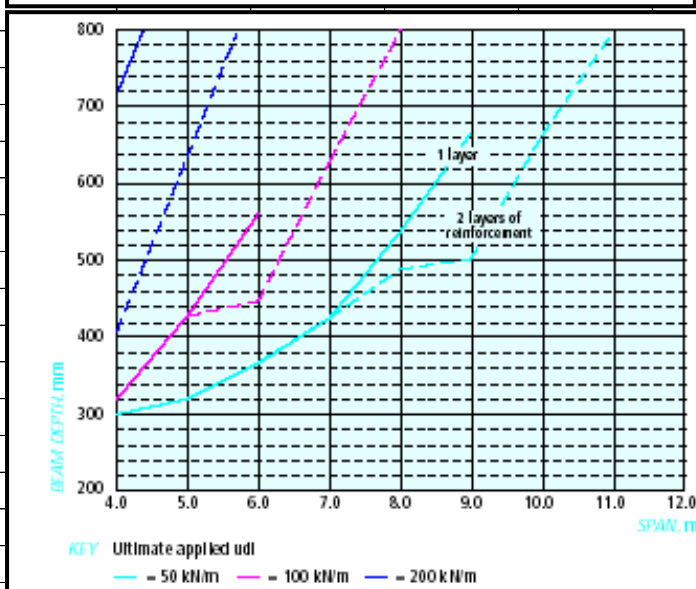
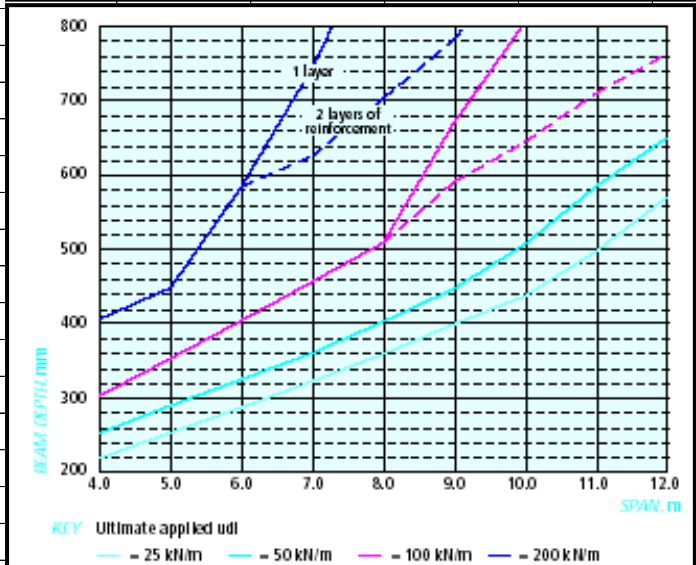
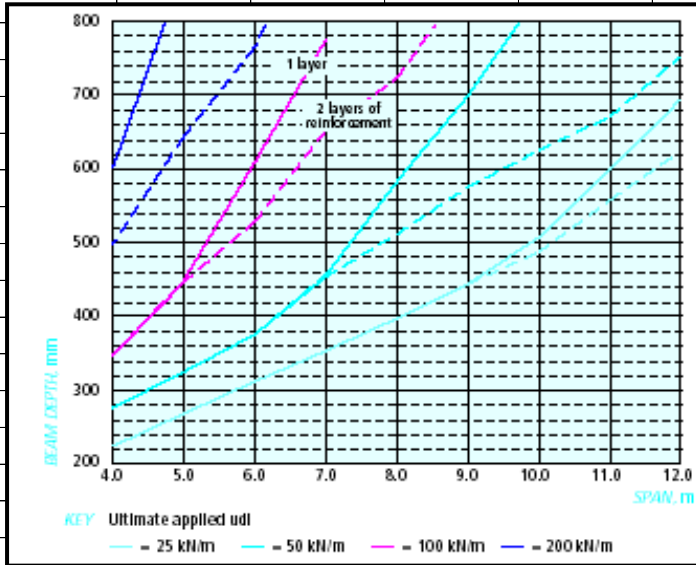


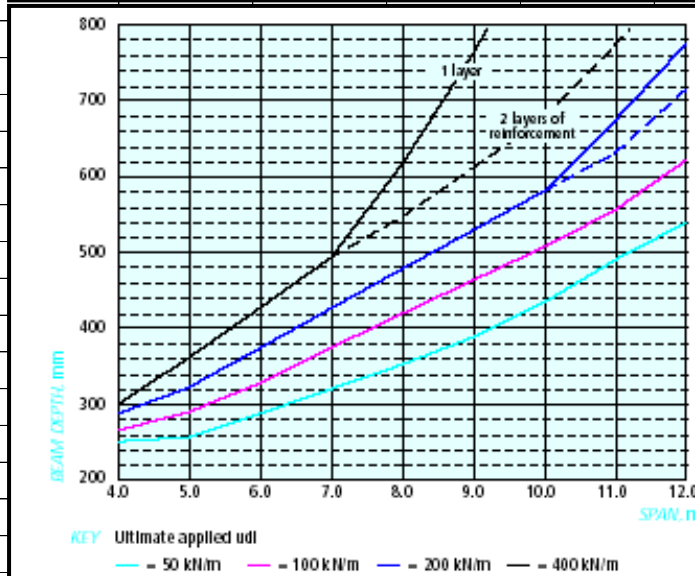
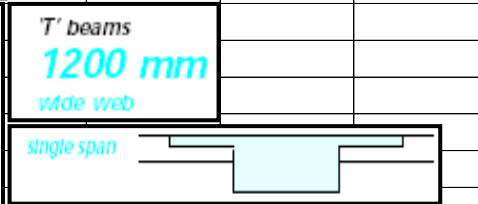
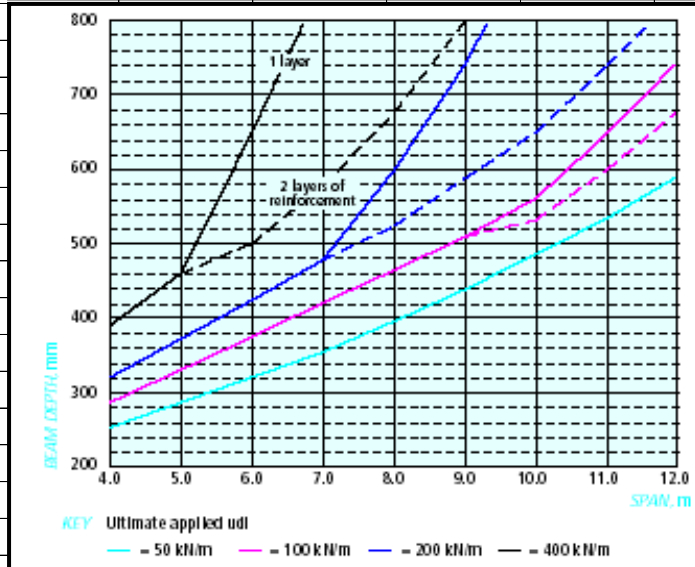
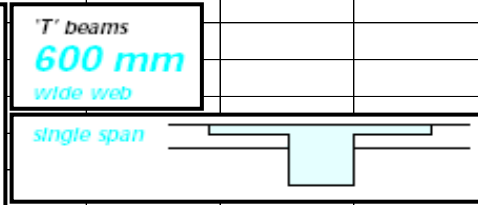
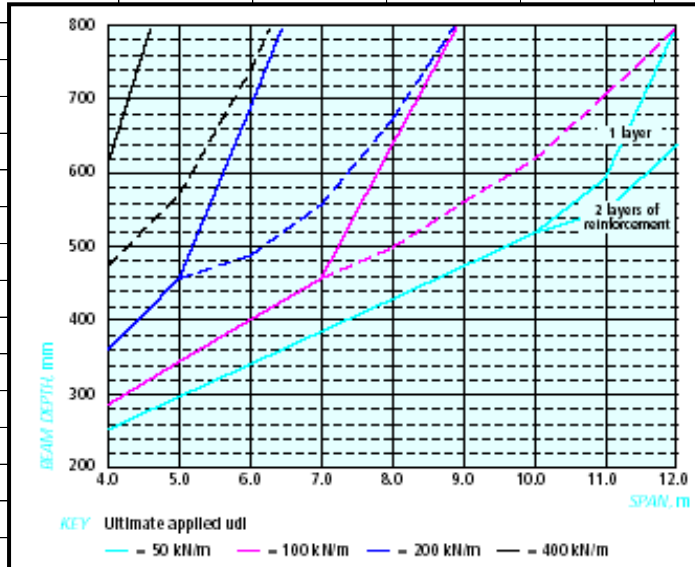
Rectangular beams

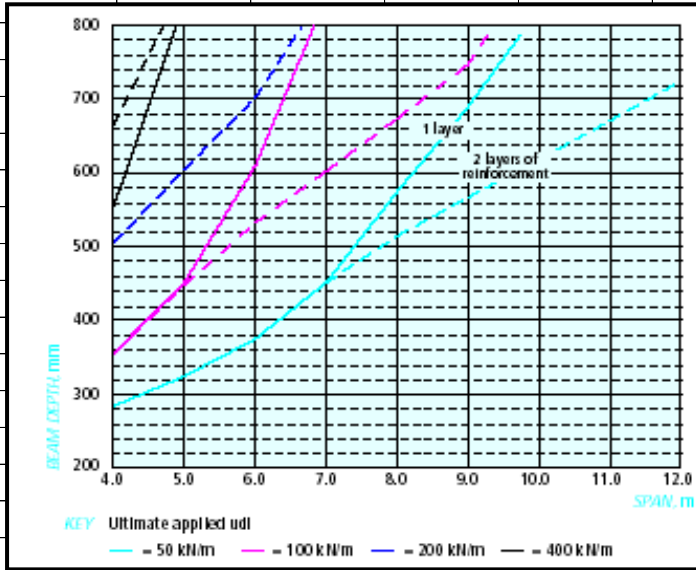
**600 mm**  
wide

single span

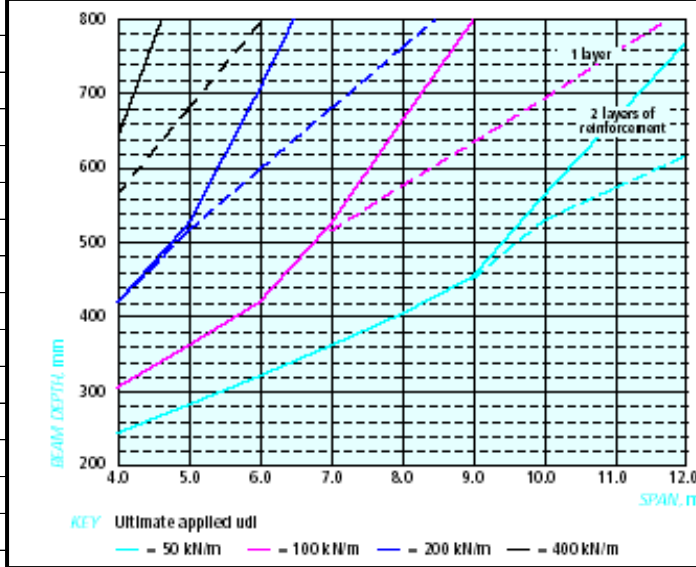




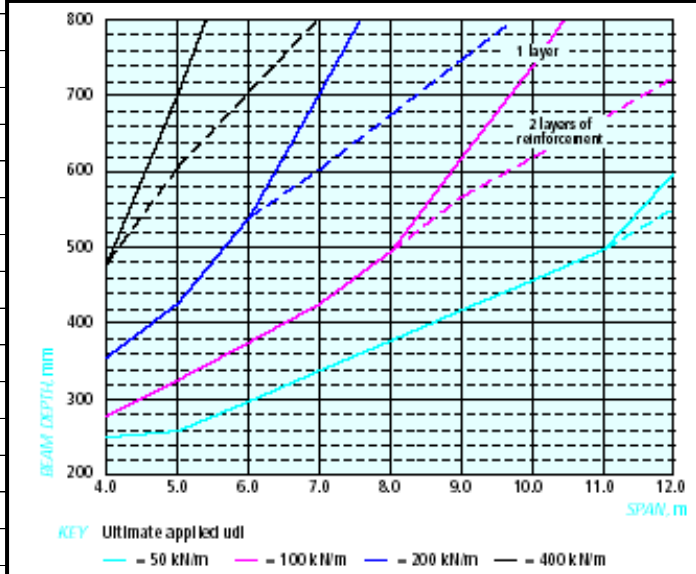
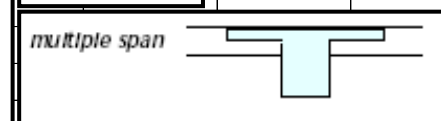




**T' beams 300 mm wide web**

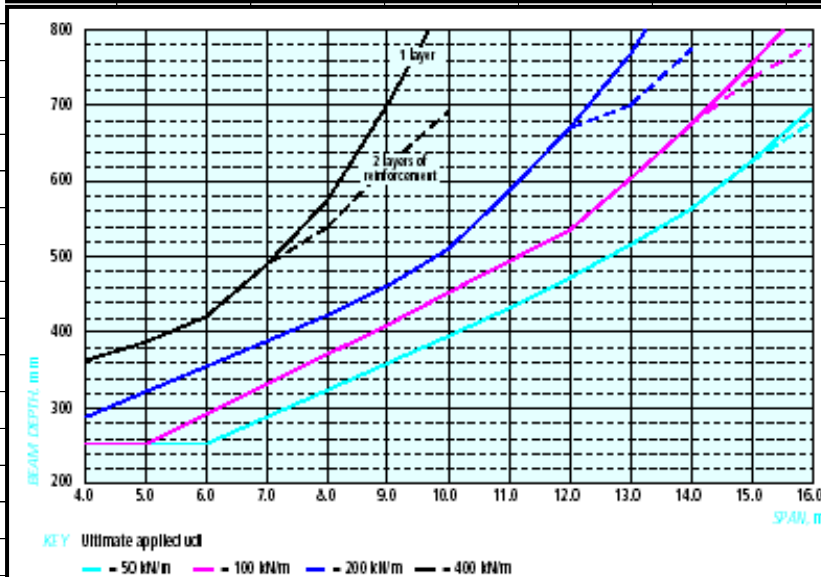
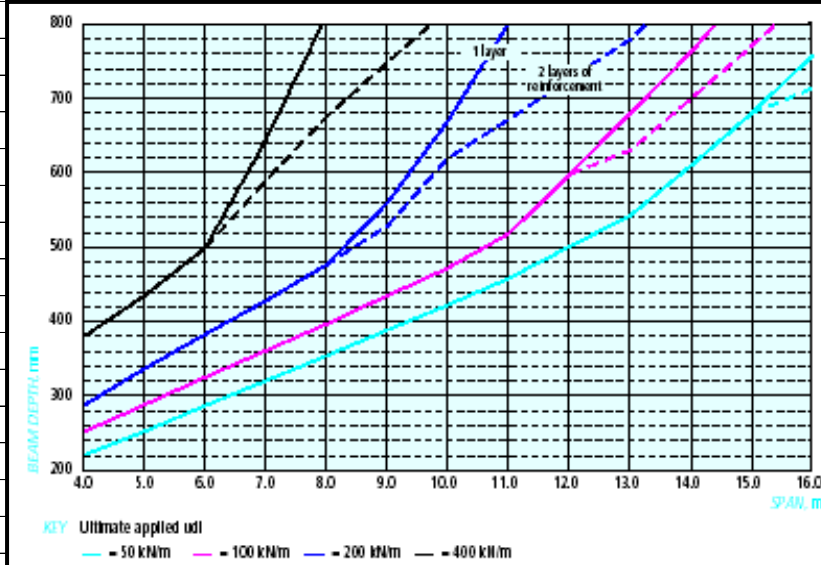
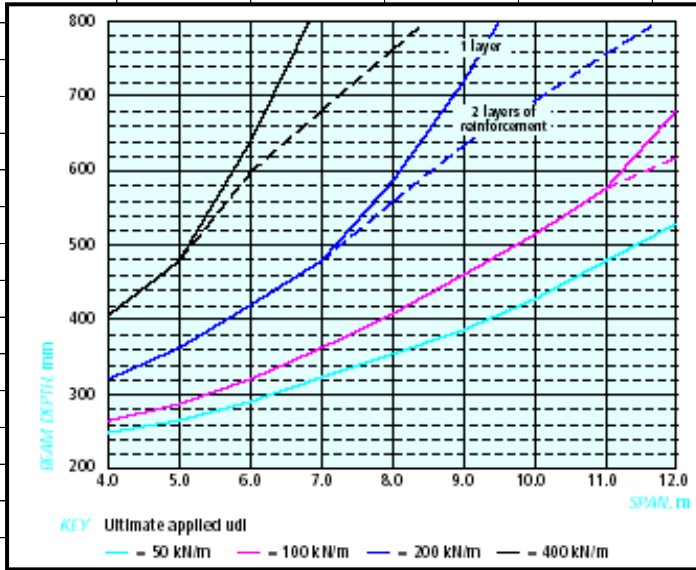


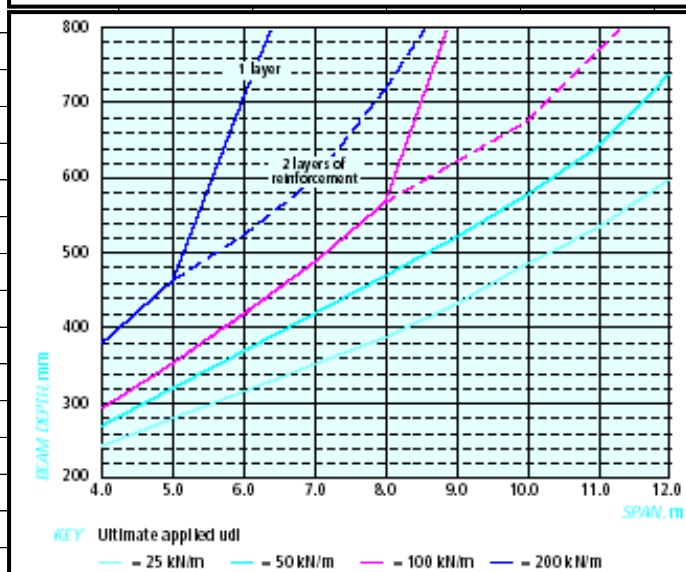
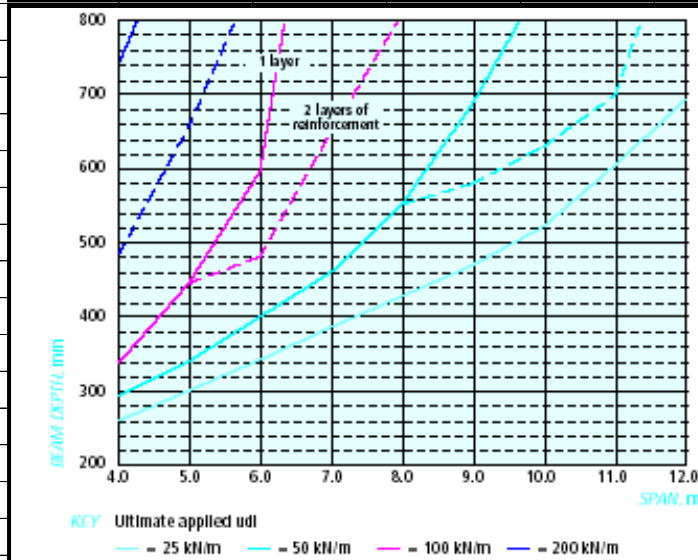
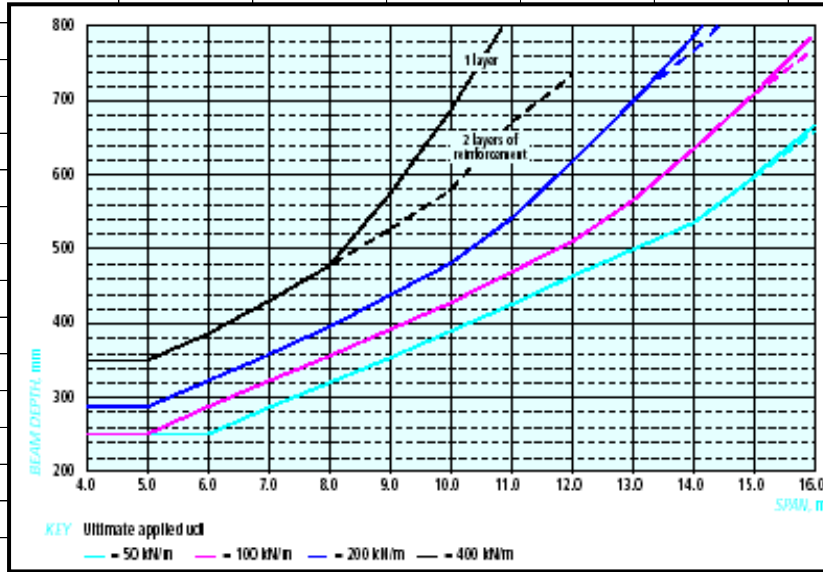
**T' beams 450 mm wide web**

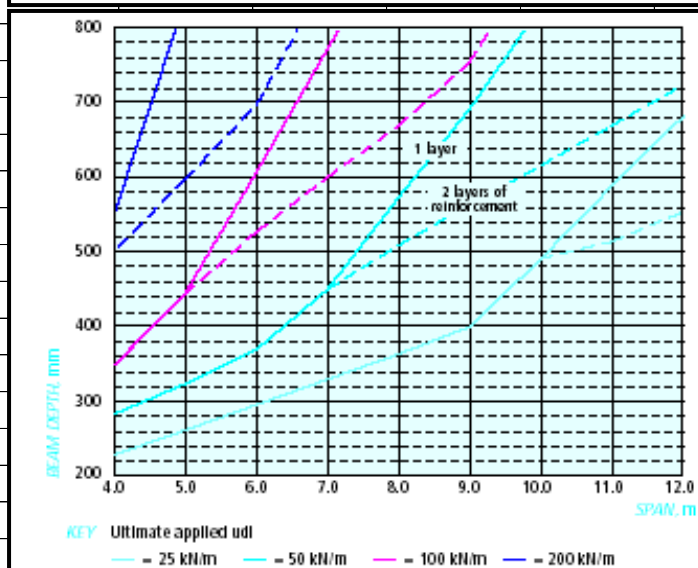
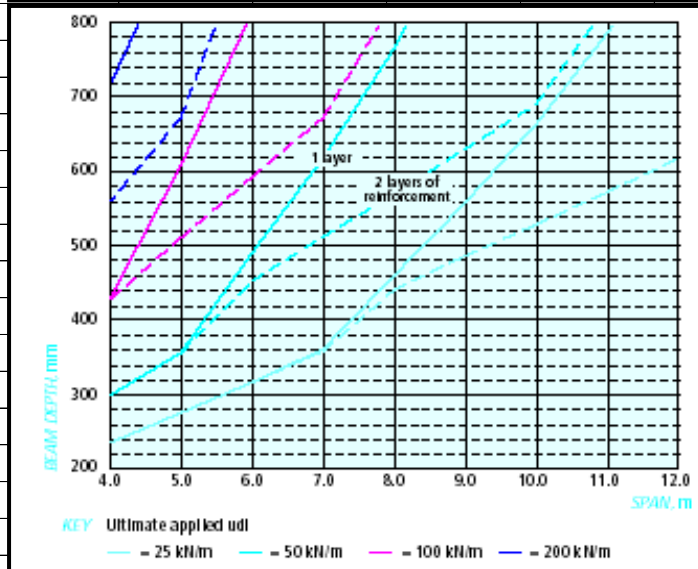
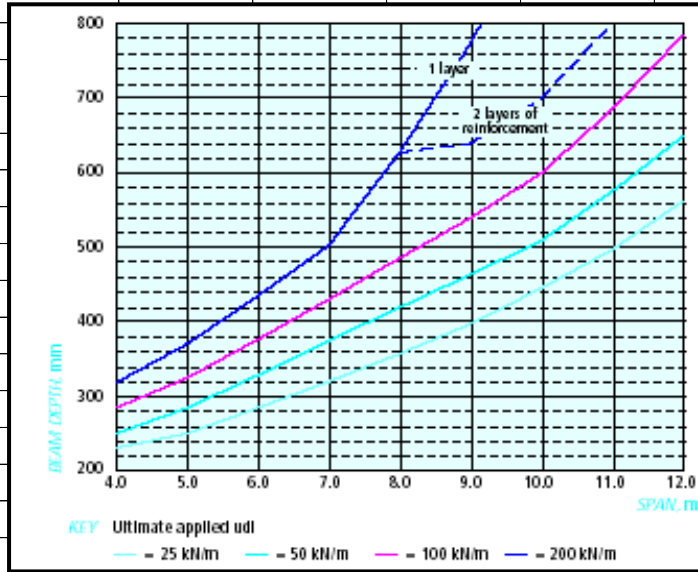


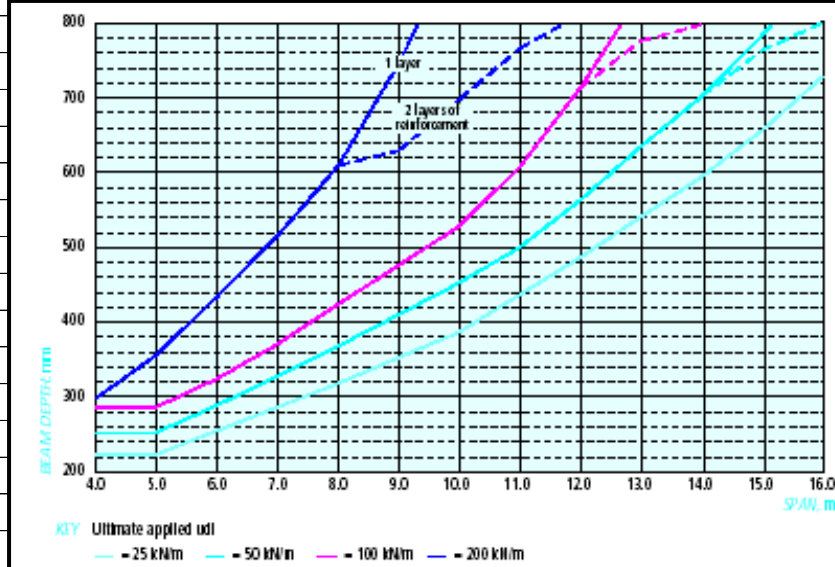
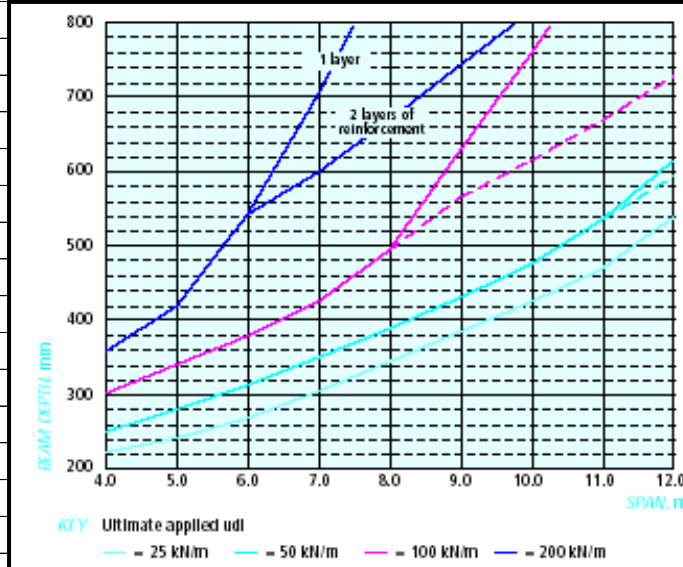
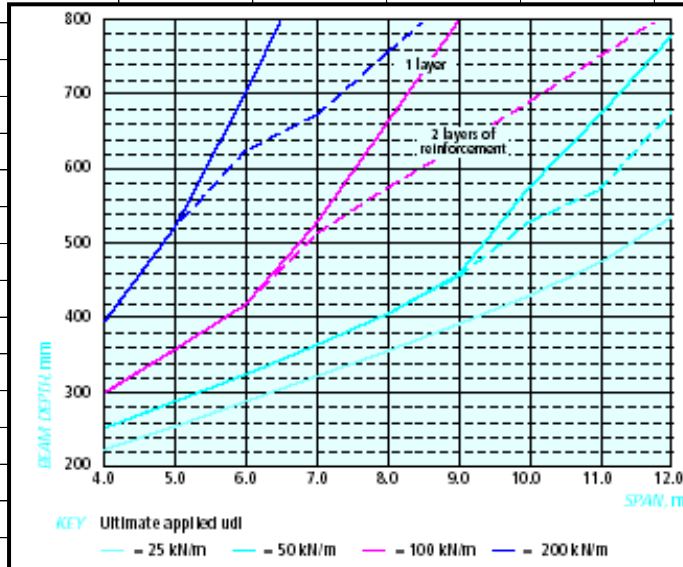
**T' beams 600 mm wide web**





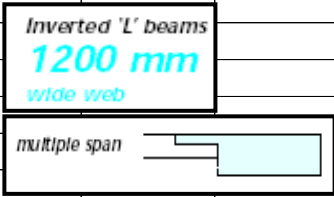
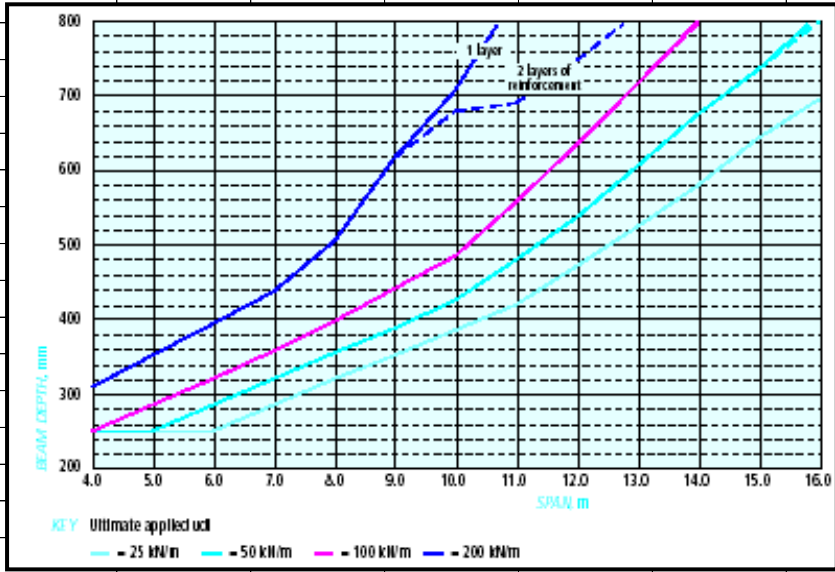








BS8110



**Table 3.1 — Allowable steel stresses in direct or flexural tension for serviceability limit states**

Design crack width mm	Allowable stress	
	Plain bars <sup>a</sup> N/mm <sup>2</sup>	Deformed bars <sup>b</sup> N/mm <sup>2</sup>
0.1	85	100
0.2	115	130

<sup>a</sup> Plain grade 250 bars complying with BS 4449.  
<sup>b</sup> Deformed grade 460 bars complying with BS 4449 or BS 4461 and high-yield wire fabric complying with BS 4483 having a guaranteed yield or proof stress and guaranteed weld strength.

*Note optional method of limiting allowable steel stress to full crack width calculation method;*

<b>CONSULTING ENGINEERS</b>	Engineering Calculation Sheet Consulting Engineers	Job No.	Sheet No.	Rev.
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Member/Location				
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Member Design - RC Beam		Made by	Date	Chd.
		XX	16/1/2024	
				<u>BS8110</u>

**Typical Initial Span / Effective Depth Ratios**

Condition	Span-to-depth ratio
Simply supported	15
End-bay	17
Cantilever	6

### Transfer beams

The experienced engineer will understand that it is not advisable to determine the section size merely by using span-to-depth tables – careful consideration is needed. Shear strength is often the governing criteria for a reinforced concrete transfer beam. From BS 8110,  $v = V/bd$ . In no case should  $v$  exceed  $0.8\sqrt{f_{cu}}$  or  $5 \text{ N/mm}^2$  (whichever is smaller). If the section is not to become congested with shear reinforcement it is advisable to limit  $v$  to  $2 \text{ N/mm}^2$ . However, it may be necessary to increase this to  $4 \text{ N/mm}^2$ . If we assume a well proportioned beam has a width,  $b$ , which is half it's depth, then we rearrange the expression above so that:

$d = \sqrt{V}$ , where  $V$  is in newtons (N) for shear stress of  $2 \text{ N/mm}^2$

$d = \sqrt{(V/2)}$  for shear stress of  $4 \text{ N/mm}^2$

The headroom under the beam should be checked and consideration given to the connection into the column. Deflection and flexural strength should also be considered because they may govern the design.

Beam span condition	Ultimate line load 25 kN/m	Ultimate line load 50 kN/m	Ultimate line load 75 kN/m
Simply supported	18	14	11
Continuous	22	17	13
Cantilever	9	7	5

Span	4m	5m	6m	7m	8m
50 kN/m UDL	250mm	300mm	350mm	400mm	500mm
100 kN/m UDL	275mm	325mm	400mm	450mm	575mm
200 kN/m UDL	325mm	375mm	450mm	525mm	650mm

Span	6m	7m	8m	9m	10m
50 kN/m UDL	250mm	300mm	350mm	400mm	475mm
100 kN/m UDL	300mm	350mm	425mm	500mm	575mm
200 kN/m UDL	350mm	400mm	475mm	575mm	675mm

<b>CONSULTING ENGINEERS</b>	Engineering Calculation Sheet Consulting Engineers	Job No.	Sheet No.	Rev.
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Member Design - RC Beam		Made by	XX
		Date	16/1/2024
			Chd.

								<u>BS8110</u>
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<b>Notes on Application to Upstand Beams</b>										
Rect - s/s		N/A						N/A		
Rect - continuous	Hog in continuous beam with precast slab						Deflections irrelevant			
Rect - cantilever	Hog in cantilever beam with precast slab						Deflections relevant			
T - s/s		N/A						N/A		
T - continuous	Hog in continuous interior beam with insitu slab						Deflections irrelevant			
T - cantilever	Hog in cantilever interior beam with insitu slab						Deflections relevant			
L - s/s		N/A						N/A		
L - continuous	Hog in continuous edge beam with insitu slab						Deflections irrelevant			
L - cantilever	Hog in cantilever edge beam with insitu slab						Deflections relevant			
Rect - s/s		Sag in s/s beam with precast or insitu slab				Deflections relevant				
Rect - continuous		Sag in continuous beam with precast or insitu slab				Deflections relevant				

book)	
ate line load 100 kN/m	
10	
12	
5	

9m	10m
575mm	675mm
675mm	800mm
775mm	925mm

11m	12m
550mm	650mm
650mm	750mm
775mm	875mm